

Correction

NEUROSCIENCE, STATISTICS

Correction for “Cluster failure: Why fMRI inferences for spatial extent have inflated false-positive rates,” by Anders Eklund, Thomas E. Nichols, and Hans Knutsson, which appeared in issue 28, July 12, 2016, of *Proc Natl Acad Sci USA* (113:7900–7905; first published June 28, 2016; 10.1073/pnas.1602413113).

The authors note that on page 7900, in the Significance Statement, lines 9–11, “These results question the validity of some 40,000 fMRI studies and may have a large impact on the interpretation of neuroimaging results” should instead appear as “These results question the validity of a number of fMRI studies and may have a large impact on the interpretation of weakly significant neuroimaging results.”

Additionally, the authors note that on page 7904, left column, fifth full paragraph, lines 1–3, “It is not feasible to redo 40,000 fMRI studies, and lamentable archiving and data-sharing practices mean most could not be reanalyzed either” should instead appear as “Due to lamentable archiving and data-sharing practices, it is unlikely that problematic analyses can be redone.”

These errors do not affect the conclusions of the article. The online version has been corrected.

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Cluster failure: Why fMRI inferences for spatial extent have inflated false-positive rates

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The most widely used task functional magnetic resonance imaging (fMRI) analyses use parametric statistical methods that depend on a variety of assumptions. In this work, we use real resting-state data and a total of 3 million random task group analyses to compute empirical familywise error rates for the fMRI software packages SPM, FSL, and AFNI, as well as a nonparametric permutation method. For a nominal familywise error rate of 5%, the parametric statistical methods are shown to be conservative for voxelwise inference and invalid for clusterwise inference. Our results suggest that the principal cause of the invalid cluster inferences is spatial autocorrelation functions that do not follow the assumed Gaussian shape. By comparison, the nonparametric permutation test is found to produce nominal results for voxelwise as well as clusterwise inference. These findings speak to the need of validating the statistical methods being used in the field of neuroimaging.

fMRI | statistics | false positives | cluster inference | permutation test

Since its beginning more than 20 years ago, functional magnetic resonance imaging (fMRI) (1, 2) has become a popular tool for understanding the human brain, with some 40,000 published papers according to PubMed. Despite the popularity of fMRI as a tool for studying brain function, the statistical methods used have rarely been validated using real data. Validations have instead mainly been performed using simulated data (3), but it is obviously very hard to simulate the complex spatiotemporal noise that arises from a living human subject in an MR scanner.

Through the introduction of international data-sharing initiatives in the neuroimaging field (4–10), it has become possible to evaluate the statistical methods using real data. Scarpazza et al. (11), for example, used freely available anatomical images from 396 healthy controls (4) to investigate the validity of parametric statistical methods for voxel-based morphometry (VBM) (12). Silver et al. (13) instead used image and genotype data from 181 subjects in the Alzheimer's Disease Neuroimaging Initiative (8, 9), to evaluate statistical methods common in imaging genetics. Another example of the use of open data is our previous work (14), where a total of 1,484 resting-state fMRI datasets from the 1,000 Functional Connectomes Project (4) were used as null data for task-based, single-subject fMRI analyses with the SPM software. That work found a high degree of false positives, up to 70% compared with the expected 5%, likely due to a simplistic temporal autocorrelation model in SPM. It was, however, not clear whether these problems would propagate to group studies. Another unanswered question was the statistical validity of other fMRI software packages. We address these limitations in the current work with an evaluation of group inference with the three most common fMRI software packages [SPM (15, 16), FSL (17), and AFNI (18)]. Specifically, we evaluate the packages in their entirety, submitting the null data to the recommended suite of preprocessing steps integrated into each package.

The main idea of this study is the same as in our previous one (14). We analyze resting-state fMRI data with a putative task design, generating results that should control the familywise error

(FWE), the chance of one or more false positives, and empirically measure the FWE as the proportion of analyses that give rise to any significant results. Here, we consider both two-sample and one-sample designs. Because two groups of subjects are randomly drawn from a large group of healthy controls, the null hypothesis of no group difference in brain activation should be true. Moreover, because the resting-state fMRI data should contain no consistent shifts in blood oxygen level-dependent (BOLD) activity, for a single group of subjects the null hypothesis of mean zero activation should also be true. We evaluate FWE control for both voxelwise inference, where significance is individually assessed at each voxel, and clusterwise inference (19–21), where significance is assessed on clusters formed with an arbitrary threshold.

In brief, we find that all three packages have conservative voxelwise inference and invalid clusterwise inference, for both one- and two-sample *t* tests. Alarming, the parametric methods can give a very high degree of false positives (up to 70%, compared with the nominal 5%) for clusterwise inference. By comparison, the nonparametric permutation test (22–25) is found to produce nominal results for both voxelwise and clusterwise inference for two-sample *t* tests, and nearly nominal results for one-sample *t* tests. We explore why the methods fail to appropriately control the false-positive risk.

Results

A total of 2,880,000 random group analyses were performed to compute the empirical false-positive rates of SPM, FSL, and AFNI; these comprise 1,000 one-sided random analyses repeated for 192 parameter combinations, three thresholding approaches,

Significance

Functional MRI (fMRI) is 25 years old, yet surprisingly its most common statistical methods have not been validated using real data. Here, we used resting-state fMRI data from 499 healthy controls to conduct 3 million task group analyses. Using this null data with different experimental designs, we estimate the incidence of significant results. In theory, we should find 5% false positives (for a significance threshold of 5%), but instead we found that the most common software packages for fMRI analysis (SPM, FSL, AFNI) can result in false-positive rates of up to 70%. These results question the validity of a number of fMRI studies and may have a large impact on the interpretation of weakly significant neuroimaging results.

Author contributions: A.E. and T.E.N. designed research; A.E. and T.E.N. performed research; A.E., T.E.N., and H.K. analyzed data; and A.E., T.E.N., and H.K. wrote the paper.

The authors declare no conflict of interest.

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See Commentary on page 7699.

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Table 1. Parameters tested for the different fMRI software packages, giving a total of 192 ($3 \times 2 \times 2 \times 4 \times 2 \times 2$) parameter combinations and three thresholding approaches

Parameter	Values used
fMRI data	Beijing (198 subjects), Cambridge (198 subjects), Oulu (103 subjects)
Block activity paradigms	B1 (10-s on off), B2 (30-s on off)
Event activity paradigms	E1 (2-s activation, 6-s rest), E2 (1- to 4-s activation, 3- to 6-s rest, randomized)
Smoothing	4-, 6-, 8-, 10-mm FWHM
Analysis type	One-sample <i>t</i> test (group activation), two-sample <i>t</i> test (group difference)
No. of subjects	20, 40
Inference level	Voxel, cluster
CDT	$P = 0.01$ ($z = 2.3$), $P = 0.001$ ($z = 3.1$)

One thousand group analyses were performed for each parameter combination.

and five tools in the three software packages. The tested parameter combinations, given in Table 1, are common in the fMRI field according to a recent review (26). The following five analysis tools were tested: SPM OLS, FSL OLS, FSL FLAME1, AFNI OLS (3dttest++), and AFNI 3dMEMA. The ordinary least-squares (OLS) functions only use the parameter estimates of BOLD response magnitude from each subject in the group analysis, whereas FLAME1 in FSL and 3dMEMA in AFNI also consider the variance of the subject-specific parameter estimates. To compare the parametric statistical methods used by SPM, FSL, and AFNI to a nonparametric method, all analyses were also performed using a permutation test (22, 23, 27). All tools were used to generate inferences corrected for the FWE rate over the whole brain.

Resting-state fMRI data from 499 healthy controls, downloaded from the 1,000 Functional Connectomes Project (4), were used for all analyses. Resting-state data should not contain systematic changes in brain activity, but our previous work (14) showed that the assumed activity paradigm can have a large

impact on the degree of false positives. Several different activity paradigms were therefore used, two block based (B1 and B2) and two event related (E1 and E2); see Table 1 for details.

Fig. 1 presents the main findings of our study, summarized by a common analysis setting of a one-sample *t* test with 20 subjects and 6-mm smoothing [see *SI Appendix, Figs. S1–S6* (20 subjects) and *SI Appendix, Figs. S7–S12* (40 subjects) for the full results]. In broad summary, parametric software's FWE rates for clusterwise inference far exceed their nominal 5% level, whereas parametric voxelwise inferences are valid but conservative, often falling below 5%. Permutation false positives are controlled at a nominal 5% for the two-sample *t* test, and close to nominal for the one-sample *t* test. The impact of smoothing and cluster-defining threshold (CDT) was appreciable for the parametric methods, with CDT $P = 0.001$ (SPM default) having much better FWE control than CDT $P = 0.01$ [FSL default; AFNI does not have a default setting, but $P = 0.005$ is most prevalent (21)].

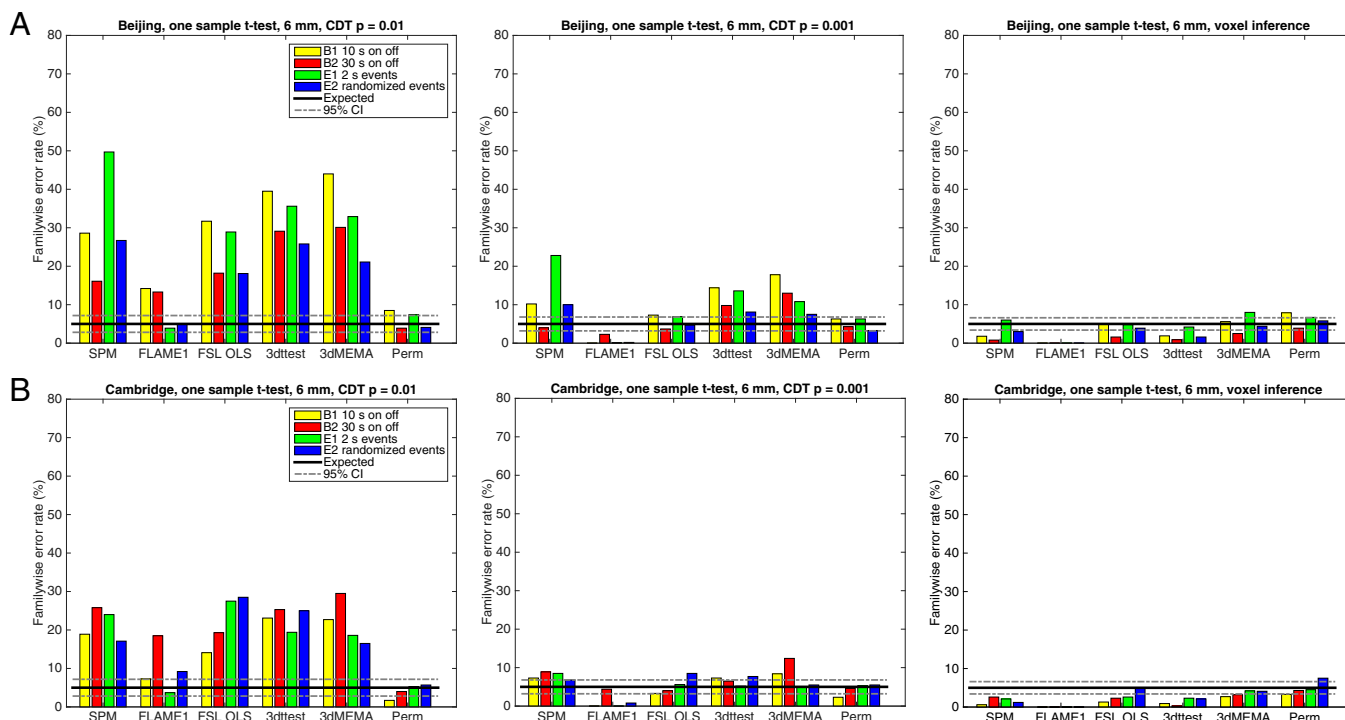


Fig. 1. Results for one-sample *t* test, showing estimated FWE rates for (A) Beijing and (B) Cambridge data analyzed with 6 mm of smoothing and four different activity paradigms (B1, B2, E1, and E2), for SPM, FSL, AFNI, and a permutation test. These results are for a group size of 20. The estimated FWE rates are simply the number of analyses with any significant group activation divided by the number of analyses (1,000). From *Left to Right*: Cluster inference using a cluster-defining threshold (CDT) of $P = 0.01$ and a FWE-corrected threshold of $P = 0.05$, cluster inference using a CDT of $P = 0.001$ and a FWE-corrected threshold of $P = 0.05$, and voxel inference using a FWE-corrected threshold of $P = 0.05$. Note that the default CDT is $P = 0.001$ in SPM and $P = 0.01$ in FSL (AFNI does not have a default setting).

Among the parametric software packages, FSL's FLAME1 clusterwise inference stood out as having much lower FWE, often being valid (under 5%), but this comes at the expense of highly conservative voxelwise inference.

We also examined an ad hoc but commonly used thresholding approach, where a CDT of $P = 0.001$ (uncorrected for multiple comparisons) is used together with an arbitrary cluster extent threshold of 10 8-mm^3 voxels (26, 28). We conducted an additional 1,000 analyses repeated for four assumed activity paradigms and the five different analysis tools (Fig. 2). Although no precise control of false positives is assured, we found this makeshift inference method had FWE ranging 60–90% for all functions except FLAME1 in FSL. Put another way, this " $P = 0.001 + 10$ voxels" method has a FWE-corrected P value of 0.6–0.9. We now seek to understand the sources of these inaccuracies.

Comparison of Empirical and Theoretical Test Statistic Distributions.

As a first step to understand the inaccuracies in the parametric methods, the test statistic values (t or z scores, as generated by each package) were compared with their theoretical null distributions. *SI Appendix, Fig. S13*, shows the histogram of all brain voxels for 1,000 group analyses. The empirical and theoretical nulls are well matched, except for FSL FLAME1, which has lower variance ($\hat{\sigma}^2 = 0.67$) than the theoretical null ($\sigma^2 = 1$). This is the proximal cause of the highly conservative results from FSL FLAME1. The mixed-effects variance is composed of intrasubject and intersubject variance ($\sigma_{WTN}^2, \sigma_{BTW}^2$, respectively), and although other software packages do not separately estimate each, FLAME1 estimates each and constrains σ_{BTW}^2 to be positive. In these null data, the true effect in each subject is zero, and thus the true $\sigma_{BTW}^2 = 0$. Thus, unless FLAME1's $\hat{\sigma}_{BTW}^2$ is correctly estimated to be 0, it can only be positively biased, and in fact this point was raised by the original authors (29).

In an follow-up analysis on FSL FLAME1 (*SI Appendix*), we conducted two-sample t tests on task fMRI data, randomly splitting subjects into two groups. In this setting, the two-sample

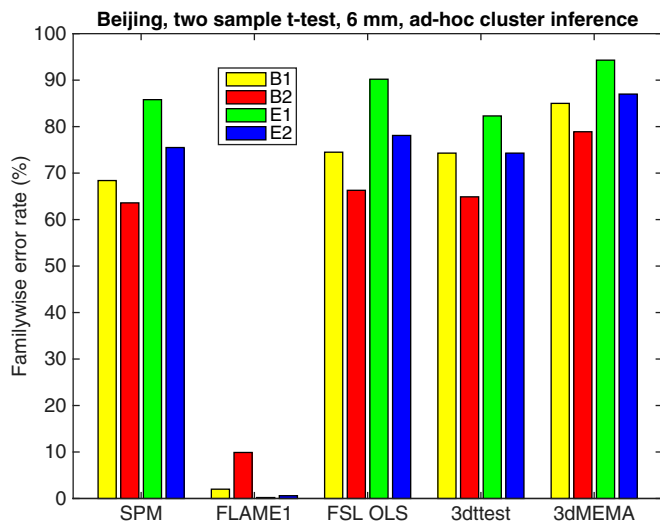


Fig. 2. Results for two-sample t test and ad hoc clusterwise inference, showing estimated FWE rates for 6 mm of smoothing and four different activity paradigms (B1, B2, E1, and E2), for SPM, FSL, and AFNI. These results were generated using the Beijing data and 20 subjects in each group analysis. Each statistic map was first thresholded using a CDT of $P = 0.001$ (uncorrected for multiple comparisons), and the surviving clusters were then compared with a cluster extent threshold of 80 mm^3 (10 voxels for SPM and FSL which used $2 \times 2 \times 2\text{ mm}^3$ voxels, three voxels for AFNI, which used $3 \times 3 \times 3\text{ mm}^3$ voxels). The estimated FWE rates are simply the number of analyses with a significant result divided by the number of analyses (1,000).

null hypothesis was still true, but $\sigma_{BTW}^2 > 0$. Here, we found cluster false-positive rates comparable to FSL OLS (44.8% for CDT $P = 0.01$ and 13.8% for CDT $P = 0.001$), supporting our conjecture of zero between-subject variance as the cause of FLAME1's conservativeness on completely null resting data.

Spatial Autocorrelation Function of the Noise. SPM and FSL depend on Gaussian random-field theory (RFT) for FWE-corrected voxelwise and clusterwise inference. However, RFT clusterwise inference depends on two additional assumptions. The first assumption is that the spatial smoothness of the fMRI signal is constant over the brain, and the second assumption is that the spatial autocorrelation function has a specific shape (a squared exponential) (30). To investigate the second assumption, the spatial autocorrelation function was estimated and averaged using 1,000 group difference maps. For each group difference map and each distance (1–20 mm), the spatial autocorrelation was estimated and averaged along x , y , and z . The empirical spatial autocorrelation functions are given in *SI Appendix, Fig. S14*. A reference squared exponential is also included for each software, based on an intrinsic smoothness of 9.5 mm (FWHM) for SPM, 9 mm for FSL, and 8 mm for AFNI (according to the mean smoothness of 1,000 group analyses, presented in *SI Appendix, Fig. S15*). The empirical spatial autocorrelation functions are clearly far from a squared exponential, having heavier tails. This may explain why the parametric methods work rather well for a high CDT (resulting in small clusters, more reflective of local autocorrelation) and not as well for a low CDT (resulting in large clusters, reflecting distant autocorrelation). *SI Appendix, Fig. S16*, shows how the cluster extent thresholds differ between the parametric and the nonparametric methods, for a CDT of $P = 0.01$. The nonparametric permutation test is valid for any spatial autocorrelation function and finds much more stringent cluster extent thresholds (three to six times higher compared with SPM, FSL, and AFNI).

To better understand the origin of the heavy tails, the spatial autocorrelation was estimated at different preprocessing stages (no preprocessing, after motion correction, after motion correction, and 6-mm smoothing) using the 198 subjects in the Beijing dataset. The resulting spatial autocorrelation functions are given in *SI Appendix, Fig. S17*. It is clear that the long tails exist in the raw data and become even more pronounced after the spatial smoothing. These long-tail spatial correlations also exist for MR phantoms (31) and can therefore be seen as scanner artifacts.

Spatial Distribution of False-Positive Clusters. To investigate whether the false clusters appear randomly in the brain, all significant clusters ($P < 0.05$, FWE-corrected) were saved as binary maps and summed together (*SI Appendix, Fig. S18*). These maps of voxelwise cluster frequency show the areas more and less likely to be marked as significant in a clusterwise analysis. Posterior cingulate was the most likely area to be covered by a cluster, whereas white matter was least likely. As this distribution could reflect variation in the local smoothness in the data, we used group residuals from 1,000 two-sample t tests to estimate voxelwise spatial smoothness (32) (*SI Appendix, Fig. S19*). The local smoothness maps show evidence of a posterior cingulate "hot spot" and reduced intensity in white matter, just as in the false-positive cluster maps. Notably, having local smoothness varying systematically with tissue type has also been observed for VBM data (13). In short, this suggests that violation of the stationary smoothness assumption may also be contributing to the excess of false positives.

In a follow-up analysis using the nonstationary toolbox for SPM (fmri.wfubmc.edu/cms/software#NS), which provides parametric cluster inference allowing for spatially varying smoothness, we calculated FWE rates for stationary as well as nonstationary smoothness. Use of nonstationary cluster size inference did not produce nominal FWE: relative to the stationary

cluster size test, it produced lower but still invalid FWE for a CDT of $P = 0.01$, and higher FWE for a CDT of $P = 0.001$ (*SI Appendix, Table S2*). This inconclusive performance can be attributed to additional assumptions and approximations introduced by the nonstationary cluster size test that can degrade its performance (33, 34). In short, we still cannot rule out heterogeneous smoothness as contributor to the standard cluster size methods' invalid performance.

Impact on a Non-Null, Task Group Analysis. All of the analyses to this point have been based on resting-state fMRI data, where the null hypothesis should be true. We now use task data to address the practical question of "How will my FWE-corrected cluster P values change?" if a user were to switch from a parametric to a nonparametric method. We use four task datasets [rhyme judgment, mixed gambles (35), living–nonliving decision with plain or mirror-reversed text, word and object processing (36)] downloaded from OpenfMRI (7). The datasets were analyzed using a parametric (the OLS option in FSL's FEAT) and a nonparametric method (the randomise function in FSL) using a smoothing of 5-mm FWHM (default option in FSL). The only difference between these two methods is that FSL FEAT-OLS relies on Gaussian RFT to calculate the corrected cluster P values, whereas randomise instead uses the data itself. The resulting cluster P values are given in *SI Appendix, Table S3* (CDT of $P = 0.01$) and *SI Appendix, Tables S4 and S5* (CDT of $P = 0.001$). *SI Appendix, Fig. S20*, summarizes these results, plotting the ratio of FWE-corrected P values, nonparametric to parametric, against cluster size. All nonparametric P values were larger than parametric (ratio > 1). Although this could be taken as evidence of a conservative nonparametric procedure, the extensive simulations showing valid nonparametric and invalid parametric cluster size inference instead suggest inflated (biased) significance in the parametric inferences. For CDT $P = 0.01$, there were 23 clusters (in 11 contrasts) with FWE parametric P values significant at $P = 0.05$ that were not significant by permutation. For CDT $P = 0.001$, there were 11 such clusters (in eight contrasts). If we assume that these mismatches represent false positives, then the empirical FWE for these 18 contrasts considered is $11/18 = 61\%$ for CDT $P = 0.01$ and $8/18 = 44\%$ for CDT $P = 0.001$. These findings indicate that the problems exist also for task-based fMRI data, and not only for resting-state data.

Permutation Test for One-Sample t Test. Although permutation tests have FWE within the expected bounds for all two-sample test results, for one-sample tests they can exhibit conservative or invalid behavior. As shown in *SI Appendix, Figs. S3, S4, S9, and S10*, the FWE can be as low as 0.8% or as high as 40%. The one-sample permutation FWE varies between site (Beijing, Cambridge, Oulu), but within each site shows a consistent pattern between the two CDTs and even for voxelwise inference. The one-sample permutation test comprises a sign flipping procedure, justified by symmetrically distributed errors (22). Although the voxel-level test statistics appear symmetric and do follow the expected parametric t distribution (*SI Appendix, Fig. S13*), the statistic values benefit from the central limit theorem and their symmetry does not imply symmetry of the data. We conducted tests of the symmetry assumption on the data for block design B1, a case suffering both spuriously low (Cambridge) and high (Beijing, Oulu) FWE (*SI Appendix*). We found very strong evidence of asymmetric errors, but with no consistent pattern of asymmetry; that is, some brain regions showed positive skew and others showed negative skew.

Discussion

Using mass empirical analyses with task-free fMRI data, we have found that the parametric statistical methods used for group fMRI analysis with the packages SPM, FSL, and AFNI can

produce FWE-corrected cluster P values that are erroneous, being spuriously low and inflating statistical significance. This calls into question the validity of countless published fMRI studies based on parametric clusterwise inference. It is important to stress that we have focused on inferences corrected for multiple comparisons in each group analysis, yet some 40% of a sample of 241 recent fMRI papers did not report correcting for multiple comparisons (26), meaning that many group results in the fMRI literature suffer even worse false-positive rates than found here (37). According to the same overview (26), the most common cluster extent threshold used is 80 mm^3 (10 voxels of size $2 \times 2 \times 2 \text{ mm}$), for which the FWE was estimated to be 60–90% (Fig. 2).

Compared with our previous work (14), the results presented here are more important for three reasons. First, the current study considers group analyses, whereas our previous study looked at single-subject analyses. Second, we here investigate the validity of the three most common fMRI software packages (26), whereas we only considered SPM in our previous study. Third, although we confirmed the expected finding of permutation's validity for two-sample t tests, we found that some settings we considered gave invalid FWE control for one-sample permutation tests. We identified skewed data as a likely cause of this and identified a simple test for detecting skew in the data. Users should consider testing for skew before applying a one-sample t test, but it remains an important area for developing new methods for one-sample analyses (see, e.g., ref. 38).

Why Is Clusterwise Inference More Problematic than Voxelwise? Our principal finding is that the parametric statistical methods work well, if conservatively, for voxelwise inference, but not for clusterwise inference. We note that other authors have found RFT clusterwise inference to be invalid in certain settings under stationarity (21, 30) and nonstationarity (13, 33). This present work, however, is the most comprehensive to explore the typical parameters used in task fMRI for a variety of software tools. Our results are also corroborated by similar experiments for structural brain analysis (VBM) (11–13, 39, 40), showing that cluster-based P values are more sensitive to the statistical assumptions. For voxelwise inference, our results are consistent with a previous comparison between parametric and nonparametric methods for fMRI, showing that a nonparametric permutation test can result in more lenient statistical thresholds while offering precise control of false positives (13, 41).

Both SPM and FSL rely on RFT to correct for multiple comparisons. For voxelwise inference, RFT is based on the assumption that the activity map is sufficiently smooth, and that the spatial autocorrelation function (SACF) is twice-differentiable at the origin. For clusterwise inference, RFT additionally assumes a Gaussian shape of the SACF (i.e., a squared exponential covariance function), that the spatial smoothness is constant over the brain, and that the CDT is sufficiently high. The 3dClustSim function in AFNI also assumes a constant spatial smoothness and a Gaussian form of the SACF (because a Gaussian smoothing is applied to each generated noise volume). It makes no assumption on the CDT and should be accurate for any chosen value. As the FWE rates are far above the expected 5% for clusterwise inference, but not for voxelwise inference, one or more of the Gaussian SACF, the stationary SACF, or the sufficiently high CDT assumptions (for SPM and FSL) must be untenable.

Why Does AFNI's Monte Carlo Approach, Unreliant on RFT, Not Perform Better? As can be observed in *SI Appendix, Figs. S2, S4, S8, and S10*, AFNI's FWE rates are excessive even for a CDT of $P = 0.001$. There are two main factors that explain these results.

First, AFNI estimates the spatial group smoothness differently compared with SPM and FSL. AFNI averages smoothness estimates from the first-level analysis, whereas SPM and FSL estimate the group smoothness using the group residuals from the general

linear model (32). The group smoothness used by 3dClustSim may for this reason be too low (compared with SPM and FSL; *SI Appendix, Fig. S15*).

Second, a 15-year-old bug was found in 3dClustSim while testing the three software packages (the bug was fixed by the AFNI group as of May 2015, during preparation of this manuscript). The bug essentially reduced the size of the image searched for clusters, underestimating the severity of the multiplicity correction and overestimating significance (i.e., 3dClustSim FWE P values were too low).

Together, the lower group smoothness and the bug in 3dClustSim resulted in cluster extent thresholds that are much lower compared with SPM and FSL (*SI Appendix, Fig. S16*), which resulted in particularly high FWE rates. We find this to be alarming, as 3dClustSim is one of the most popular choices for multiple-comparisons correction (26).

We note that FWE rates are lower with the bug-fixed 3dClustSim function. As an example, the updated function reduces the degree of false positives from 31.0% to 27.1% for a CDT of $P = 0.01$, and from 11.5% to 8.6% for a CDT of $P = 0.001$ (these results are for two-sample t tests using the Beijing data, analyzed with the E2 paradigm and 6-mm smoothing).

Suitability of Resting-State fMRI as Null Data for Task fMRI. One possible criticism of our work is that resting-state fMRI data do not truly compromise null data, as they may be affected by consistent trends or transients, for example, at the start of the session. However, if this were the case, the excess false positives would appear only in certain paradigms and, in particular, least likely in the randomized event-related (E2) design. Rather, the inflated false positives were observed across all experiment types with parametric cluster size inference, limiting the role of any such systematic effects. Additionally, one could argue that the spatial structure of resting fMRI, the very covariance that gives rise to “resting-state networks,” is unrepresentative of task data and inflates the spatial autocorrelation functions and induces nonstationarity. We do not believe this is the case because it has been shown that resting-state networks can be estimated from the residuals of task data (42), suggesting that resting data and task noise share similar properties. We assessed this in our four task datasets, estimating the spatial autocorrelation of the group residuals (*SI Appendix, Fig. S21*) and found the same type of heavy-tailed behavior as in the resting data. Furthermore, the same type of heavy-tail spatial autocorrelation has been observed for data collected with an MR phantom (31). Finally, another follow-up analysis on task data (see *Comparison of Empirical and Theoretical Test Statistic Distributions* and *SI Appendix, Task-Based fMRI Data, Human Connectome Project*, a two-sample t test on a random split of a homogeneous group of subjects) found inflated false-positive rates similar to the null data. Altogether, we find that these findings support the appropriateness of resting data as a suitable null for task fMRI.

The Future of fMRI. Due to lamentable archiving and data-sharing practices, it is unlikely that problematic analyses can be redone. Considering that it is now possible to evaluate common statistical methods using real fMRI data, the fMRI community should, in our opinion, focus on validation of existing methods. The main drawback of a permutation test is the increase in computational complexity, as the group analysis needs to be repeated 1,000–10,000 times. However, this increased processing time is not a problem in practice, as for typical sample sizes a desktop

computer can run a permutation test for neuroimaging data in less than a minute (27, 43). Although we note that metaanalysis can play an important role in teasing apart false-positive findings from consistent results, that does not mitigate the need for accurate inferential tools that give valid results for each and every study.

Finally, we point out the key role that data sharing played in this work and its impact in the future. Although our massive empirical study depended on shared data, it is disappointing that almost none of the published studies have shared their data, neither the original data nor even the 3D statistical maps. As no analysis method is perfect, and new problems and limitations will be certainly found in the future, we commend all authors to at least share their statistical results [e.g., via [NeuroVault.org](https://neurovault.org) (44)] and ideally the full data [e.g., via [OpenfMRI.org](https://openfmri.org) (7)]. Such shared data provide enormous opportunities for methodologists, but also the ability to revisit results when methods improve years later.

Materials and Methods

Only publicly shared anonymized fMRI data were used in this study. Data collection at the respective sites was subject to their local ethics review boards, who approved the experiments and the dissemination of the anonymized data. For the 1,000 Functional Connectomes Project, collection of the Cambridge data was approved by the Massachusetts General Hospital partners' institutional review board (IRB); collection of the Beijing data was approved by the IRB of State Key Laboratory for Cognitive Neuroscience and Learning, Beijing Normal University; and collection of the Oulu data was approved by the ethics committee of the Northern Ostrobothnian Hospital District. Dissemination of the data was approved by the IRBs of New York University Langone Medical Center and New Jersey Medical School (4). The word and object processing experiment (36) was approved by the Berkshire National Health Service Research Ethics Committee. The mixed-gambles experiment (35), the rhyme judgment experiment, and the living–nonliving experiments were approved by the University of California, Los Angeles, IRB. All subjects gave informed written consent after the experimental procedures were explained.

The resting-state fMRI data from the 499 healthy controls were analyzed in SPM, FSL, and AFNI according to standard processing pipelines, and the analyses were repeated for four levels of smoothing (4-, 6-, 8-, and 10-mm FWHM) and four task paradigms (B1, B2, E1, and E2). Random group analyses were then performed using the parametric functions in the three softwares (SPM OLS, FLAME1, FSL OLS, 3dttest, 3dMEMA) as well as the nonparametric permutation test. The degree of false positives was finally estimated as the number of group analyses with any significant result, divided by the number of group analyses (1,000). All of the processing scripts are available at <https://github.com/wanderine/ParametricMultisubjectfMRI>.

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Supporting Information Appendix

Cluster failure: Why fMRI inferences for spatial extent have inflated false positive rates

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Methods

Resting state fMRI data

Resting state fMRI data from 499 healthy controls were downloaded from the 1000 functional connectomes project [1] (http://fcon_1000.projects.nitrc.org/fcpClassic/FcpTable.html). The Beijing, Cambridge, and Oulu datasets were selected for their large sample sizes (198, 198 and 103 subjects respectively) and their narrow age ranges (Beijing: 18 - 26 years, mean 21.16, SD 1.83, Cambridge: 18 - 30 years, mean 21.03, SD 2.31, Oulu: 20 - 23 years, mean 21.52, SD 0.57). For the Beijing data, there are 76 male and 122 female subjects. For the Cambridge data, there are 75 male and 123 female subjects. For the Oulu data, there are 37 male and 66 female subjects. Three Tesla (T) MR scanners were used for the Beijing as well as for the Cambridge data, while a 1.5 T scanner was used for the Oulu data.

The Beijing data were collected with a repetition time (TR) of 2 seconds and consist of 225 time points per subject, $64 \times 64 \times 33$ voxels of size $3.125 \times 3.125 \times 3.6 \text{ mm}^3$. The Cambridge data were collected with a TR of 3 seconds and consist of 119 time points per subject, $72 \times 72 \times 47$ voxels of size $3 \times 3 \times 3 \text{ mm}^3$. The Oulu data were collected for with a TR of 1.8 seconds and consist of 245 time points per subject, $64 \times 64 \times 28$ voxels of size $4 \times 4 \times 4.4 \text{ mm}$. For each subject there is one T_1 -weighted anatomical volume which can be used for normalization to a brain template. According to the motion plots from FSL, four Oulu subjects moved slightly more than 1 mm in any direction. According to motion plots from AFNI, one Cambridge subject, three Beijing subjects and eight Oulu subjects moved slightly more than 1 mm. The fMRI data have not been corrected for geometric distortions, and no field maps are available for this purpose.

We randomly selected subsets of subjects for one sample t-tests (group activation) and two-sample t-tests (group difference). Since the subjects were not performing any task and all are healthy and of similar age, the number of analyses with one or more significant effects should follow the nominal rate (analyses were performed separately for Beijing, Cambridge and Oulu). The same approach has previously been used to test the validity of parametric statistics for voxel based morphometry [2, 3].

Random group generation

Each random group was created by first applying a random permutation to a list containing all the 198, or 103, subject numbers. To create two random groups of 20 subjects each, the first 20 permuted subject numbers were put into group 1, and the following 20 permuted subject numbers were put into group 2. According to the n choose k formula $\frac{n!}{k!(n-k)!}$ it is possible to create approximately $1.31 \cdot 10^{42}$ such random group divisions (for $n = 198$ and $k = 40$). This collection of random analyses is

not independent, but the estimate of the familywise false positive rate is unbiased (as the expectation operator is additive under dependence). A total of 1,000 random analyses were used to estimate the FWE (the same 1,000 analyses for all softwares and all parameter combinations), for which the normal approximation of the Binomial 95% confidence interval is 3.65% - 6.35% for a nominal FWE of 5%. Since the independence assumption of this normal approximation does not hold, we conducted Monte Carlo simulations to assess its accuracy (see Supplementary Table 1).

Supplementary Table 1: Monte Carlo simulations on the accuracy of normal approximation for Binomial 95% confidence intervals, to address the dependence in the 1,000 subgroups drawn from 103 or 198 subjects. Normally distributed noise volumes (103 or 198 volumes, 60 x 60 x 60 voxels of size 2 x 2 x 2 mm, no mask) were generated and smoothed with 10 mm FWHM, and random subsets of $n = 20$ or 40 volumes were drawn, 1,000 times, and used to construct one-sample t-tests. Inference was performed using cluster inference, with a CDT of $p = 0.01$ or 0.001, as well as voxel inference. This entire process was repeated 1,000 times. The voxel and cluster size FWE thresholds were determined from a separate Monte Carlo simulation (10,000 realizations). We found that results with more smoothing resulted in more inflated confidence intervals, and hence only show the worst case 10 mm FWHM results here.

Number of subjects	Sample size	Inference	95% CI
103	20	Voxel	3.40% - 7.00%
103	20	Cluster, CDT $p = 0.001$	3.00% - 7.80%
103	20	Cluster, CDT $p = 0.01$	2.50% - 8.70%
103	40	Voxel	2.40% - 9.30%
103	40	Cluster, CDT $p = 0.001$	1.90% - 11.30%
103	40	Cluster, CDT $p = 0.01$	1.50% - 13.50%
198	20	Voxel	3.40% - 6.60%
198	20	Cluster, CDT $p = 0.001$	3.20% - 6.80%
198	20	Cluster, CDT $p = 0.01$	2.80% - 7.20%
198	40	Voxel	3.10% - 6.90%
198	40	Cluster, CDT $p = 0.001$	2.50% - 7.50%
198	40	Cluster, CDT $p = 0.01$	2.00% - 8.00%

Code availability

Parametric group analyses were performed using SPM 8 (<http://www.fil.ion.ucl.ac.uk/spm/software/spm8/>), FSL 5.0.7 (<http://fsl.fmrib.ox.ac.uk/fsldownloads/>) and AFNI (<http://afni.nimh.nih.gov/afni/download/afni/releases>, compiled August 13 2014, version 2011_12_21_1014). FSL can perform non-parametric group analyses using the function `randomise`, but we here used our BROCCOLI software [4] (<https://github.com/wanderine/BROCCOLI>) to lower the processing time. All the processing scripts are freely available (<https://github.com/wanderine/ParametricMultisubjectfMRI>) to show all the processing settings and to facilitate replication of the results. Since all the software packages and all the fMRI data are also freely available, anyone can replicate the results in this paper.

First level analyses

A processing script was used for each software package to perform first level analyses for each subject, resulting in brain activation maps in a standard brain space (Montreal Neurological Institute (MNI) for SPM and FSL, and Talairach for AFNI).

All first level analyses involved normalization to a brain template, motion correction and different amounts of smoothing (4, 6, 8 and 10 mm full width at half maximum). Slice timing correction was not performed, as the slice timing information is not available for these fMRI datasets. A general linear model (GLM) was applied to the preprocessed fMRI data, using different regressors for activity (B1, B2, E1, E2). The estimated head motion parameters were used as additional regressors in the design matrix, for all packages, to further reduce effects of head motion.

First level analyses for SPM were performed using a Matlab batch script, closely following the SPM manual. The spatial normalization was done as a two step procedure, where the mean fMRI volume was first aligned to the anatomical volume (using the function 'Coregister' with default settings). The anatomical volume was aligned to MNI space using the function 'Segment' (with default settings), and the two transforms were finally combined to transform the fMRI data to MNI space at 2 mm isotropic resolution (using the function 'Normalise: Write'). Spatial smoothing was finally applied to the spatially normalized fMRI data. The first level models were then fit in the atlas space, i.e. not in the subject space.

For FSL, first level analyses were setup through the FEAT GUI. The spatial normalization to the brain template (MNI152_T1_2mm_brain.nii.gz) was performed as a two step linear registration using the function FLIRT (which is the default option). One fMRI volume was aligned to the anatomical volume using the BBR (boundary based registration) option in FLIRT (default). The anatomical volume was aligned to MNI space using a linear registration with 12 degrees of freedom (default), and the two transforms were finally combined. The first level models were fit in the subject space (after spatial smoothing), and the contrasts and their variances were then transformed to the atlas space.

First level analyses in AFNI were performed using the standardized processing script `afni_proc.py`, which creates a `tchsh` script which contains all the calls to different AFNI functions. The spatial normalization to Talairach space was performed as a two step procedure. One fMRI volume was first linearly aligned to the anatomical volume, using the script `align_epi_anat.py`. The anatomical volume was then linearly aligned to the brain template (TT_N27+tlrc) using the script `@auto_tlrc`. The transformations from the spatial normalization and the motion correction were finally applied using a single interpolation, resulting in normalized fMRI data in an isotropic resolution of 3 mm. Spatial smoothing was applied to the spatially normalized fMRI data, and the first level models were then fit in the atlas space (i.e. not in the subject space).

Default drift modeling or highpass filtering options were used in each of SPM, FSL and AFNI. A discrete cosine transform with cutoff of 128 seconds was used for SPM, while highpass filters with different cutoffs were used for FSL (20 seconds for activity paradigm B1, 60 seconds for B2 and 100 seconds for E1 and E2), matching the defaults used by the FEAT GUI, and AFNI's Legendre polynomial order is 4 and 3 for the Beijing and the Cambridge data, respectively (based on total scan duration). Temporal correlations were further corrected for with a global AR(1) model in SPM, an arbitrary temporal autocorrelation function regularized with a Tukey taper and adaptive spatial smoothing in FSL and a voxel-wise ARMA(1,1) model in AFNI.

Group analyses

A second processing script was used for each software package to perform random effect group analyses, using the results from the first level analyses. For SPM, group analyses were only performed with the resulting beta weights from the first level analyses, using ordinary least squares (OLS) regression over subjects. For FSL, group analyses were performed both using FLAME1 (which is the default option) and OLS. The FLAME1 function uses both the beta weight and the corresponding variance of each subject, subsequently estimating a between subject variance. For AFNI, group analyses were performed using the functions 3dttest++ (OLS, using beta estimates from the function 3dDeconvolve which assumes independent errors) and 3dMEMA (which is similar to FLAME1 in FSL, using beta and variance estimates from the function 3dREMLfit which uses a voxel-wise ARMA(1,1) model of the errors).

For the non-parametric analyses in BROCCOLI, first level results from FSL were used with OLS regression. A one-sample permutation test on measures of change (i.e. BOLD contrast images) is conducted by randomly flipping the sign of each subject's data. Also known as the wild bootstrap, this is an exact test when the errors at each voxel are symmetrically distributed [5]. A two-sample permutation test proceeds by randomly re-assigning group labels to subjects. Each non-parametric group analysis was performed using 1,000 permutations or sign flips, a random sample of the millions of possible sign-flips and permutations. For each permutation the maximal test statistic (voxel statistic or cluster size) over the brain is retained, creating the null maximum distribution used for FWE inference.

Voxel-wise FWE-corrected p-values from SPM and FSL were obtained based on their respective implementations of random field theory [6], while AFNI FWE p-values were obtained with a Bonferroni correction for the number of voxels (AFNI does not provide any specific program for voxel-wise FWE p-values). For the non-parametric analyses, FWE-corrected p-values were calculated as the proportion of the maximum statistic null distribution being as large or larger than a given statistic value.

Cluster-wise FWE-corrected p-values from SPM and FSL were likewise obtained based on their implementations of random field theory [7]. AFNI estimates FWE p-values with a simulation based procedure, 3dClustSim [8]. SPM and FSL estimate smoothness from the residuals of the group level analysis (used for both voxel-wise and cluster-wise inference), while AFNI uses the average of the first level analyses' smoothness estimates. For the non-parametric analyses, FWE-corrected p-values were calculated as the proportion of the maximum cluster size null distribution being as large or larger than a given cluster's size.

Each group analysis was considered to give a significant result if any cluster or voxel had a FWE-corrected p-value $p < 0.05$.

Symmetry assumption for permutation based one-sample t-test

The permutation based one-sample t-test requires that the errors are symmetrically distributed. To investigate this assumption, voxel-wise skewness s was estimated according to

$$s = \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^3}{\left(\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 \right)^{3/2}}, \quad (1)$$

where n is the number of subjects in each group analysis and x_i represents the first level activity estimate for subject i . For each random group analysis a sign flipping test (with 100 sign flips) was used to calculate voxel-wise p-values of skewness. The voxel-wise mean was removed prior to the sign flipping, and the maximum and minimum skewness values across the entire brain were saved for each sign flip to form the maximum and minimum null distributions (required to calculate corrected p-values).

Testing 100 random one-sample $n = 20$ group analyses for skew, the vast majority of analyses had evidence for both positive and negative skew. For the Beijing datasets analyzed with paradigm B1, 82 analyses had 5% FWE-significant positive skew, 86 significant negative skew; for Cambridge B1, 91 analyses had significant negative skew, 72 significant positive skew; for Oulu B1, 99 analyses had significant positive skew and 94 significant negative skew. A given voxel cannot be both positively and negatively skewed, but rather these results show that both positively and negatively skewed voxels are prevalent in all three datasets. Interestingly, the skewness varies both with the spatial location and the assumed activity paradigm.

Why is cluster-wise inference more problematic than voxelwise?

Supplementary Figure 14 shows that the SACFs are far from a squared exponential. The empirical SACFs are close to a squared exponential for small distances, but the autocorrelation is higher than expected for large distances. This could be the reason why the parametric methods work rather well for a high cluster defining threshold ($p = 0.001$), and not at all for a low threshold ($p = 0.01$). A low threshold gives large clusters with a large radius, for which the tail of the SACF is quite important. For a high threshold, resulting in rather small clusters with a small radius, the tail is not as important. Also, it could simply be that the high-threshold assumption is not satisfied for a CDT of $p = 0.01$. Supplementary Figure 19 shows that the spatial smoothness is not constant in the brain, but varies spatially. Note that the bright areas match the spatial distribution of false clusters in Supplementary Figure 18; it is more likely to find a large cluster for a high smoothness. The permutation test does not assume a specific shape of the SACF, nor does it assume a constant spatial smoothness, nor require a high CDT. For these reasons, the permutation test provides valid results, for two sample t-tests, for both voxel and cluster-wise inference.

Which parameters affect the familywise error rate for cluster-wise inference?

The cluster defining threshold is the most important parameter for SPM, FSL and AFNI; using a more liberal threshold increases the degree of false positives. This result is consistent with previous work [9, 10, 11]. However, the permutation test is completely unaffected by changes of this parameter. According to a recent review looking at 484 fMRI studies [10], the CDT used varies greatly between the three software packages (mainly due to different default settings). SPM and FSL have default thresholds of $p = 0.001$ and $p = 0.01$, respectively; while AFNI has no default setting, $p = 0.005$ is most prevalent.

The amount of smoothing has a rather large impact on the degree of false positives, especially for FSL OLS. The results from the permutation test, on the other hand, do not depend on this parameter. The original fMRI data has an intrinsic SACF, which is combined with the SACF of the smoothing kernel. The final SACF will more closely resemble a squared exponential for high levels of smoothing, simply because the smoothing operation forces the data to have a more Gaussian SACF. The permutation test does not assume a specific form of the SACF, and therefore performs well for any degree of smoothing.

All software packages are affected by the analysis type; the familywise error rates are generally lower for a two-sample t-test compared to a one sample t-test. This is a reflection of the greater robustness of the two-sample t-test: a difference of two variables (following the same distribution) has a symmetric distribution, which is an important facet of a normal distribution.

Task based fMRI data

OpenfMRI

Task based fMRI data were downloaded from the OpenfMRI project [12] (<http://openfmri.org>), to investigate how cluster based p-values differ between parametric and non-parametric group analyses. Each task dataset contains fMRI data, anatomical data and timing information for each subject. The datasets were only analyzed with FSL, using 5 mm of smoothing (the default option). Motion regressors were used in all cases, to further suppress effects of head motion. Group analyses were performed using the parametric OLS option (i.e. not the default FLAME1 option) and the non-parametric randomise function (which performs OLS regression in each permutation).

Rhyme judgment

The rhyme judgment dataset is available at <http://openfmri.org/dataset/ds000003>. The 13 subjects (8 male, age range 18 - 38 years, mean 24.08, SD 6.52) were presented with pairs of either words or pseudo words and made rhyming judgments for each pair. The design contains four 20 second blocks per category, with eight 2 second events in each block (each block is separated with 20 seconds of rest). The fMRI data were collected with a repetition time of 2 seconds and consist of 160 time points per subject, the spatial resolution is $3.125 \times 3.125 \times 4 \text{ mm}^3$ (resulting in volumes of $64 \times 64 \times 33$ voxels). The data were analyzed with two regressors; one for words and one for pseudo words. A total of four contrasts were applied; words, pseudowords,

words - pseudo words, pseudo words - words. For a cluster defining threshold of $p = 0.01$, a t-threshold of 2.65 was used. For a cluster defining threshold of $p = 0.001$, a t-threshold of 3.95 was used.

Mixed-gambles task

The mixed-gambles task dataset is available at <http://openfmri.org/dataset/ds000005>. The 16 subjects (8 male, age range 19 - 28 years, mean 22.06, SD 2.86) were presented with mixed (gain/loss) gambles, in an event related design, and decided whether they would accept each gamble. No outcomes of these gambles were presented during scanning, but after the scan three gambles were selected at random and played for real money. The fMRI data were collected using a 3 T Siemens Allegra scanner. A repetition time of 2 seconds was used and a total of 240 volumes were collected for each run, the spatial resolution is $3.125 \times 3.125 \times 4 \text{ mm}^3$ (resulting in volumes of $64 \times 64 \times 34$ voxels). The dataset contains three runs per subject, but only the first run was used in our analysis. The data were analyzed using four regressors; task, parametric gain, parametric loss and distance from indifference. A total of four contrasts were applied; parametric gain, - parametric gain, parametric loss, - parametric loss. For a cluster defining threshold of $p = 0.01$, a t-threshold of 2.57 was used. For a cluster defining threshold of $p = 0.001$, a t-threshold of 3.75 was used.

Living-nonliving decision with plain or mirror-reversed text

The living-nonliving decision task dataset is available at <http://openfmri.org/dataset/ds000006a>. The 14 subjects (5 male, age range 19 - 35 years, mean 22.79, SD 4.00) made living-nonliving decisions, in an event related design, on items presented in either plain or mirror-reversed text. The fMRI data were collected using a 3 T Siemens Allegra scanner. A repetition time of 2 seconds was used and a total of 205 volumes were collected for each run, the spatial resolution is $3.125 \times 3.125 \times 5 \text{ mm}^3$ (resulting in volumes of $64 \times 64 \times 25$ voxels). The dataset contains six runs per subject, but only the first run was used in our analysis. The data were analyzed using five regressors; mirror-switched, mirror-nonswitched, plain-switched, plain-nonswitched and junk. A total of four contrasts were applied; mirrored versus plain (1,1,-1,-1,0), switched versus non-switched (1,-1,1,-1,0), switched versus non-switched mirrored only (1,-1,0,0,0) and switched versus non-switched plain only (0,0,1,-1,0). For a cluster defining threshold of $p = 0.01$, a t-threshold of 2.615 was used. For a cluster defining threshold of $p = 0.001$, a t-threshold of = 3.87 was used.

Word and object processing

The word and object processing task dataset is available at <http://openfmri.org/dataset/ds000107>. The 49 subjects (age range 19 - 38 years, mean 25) performed a visual one-back task with four categories of items: written words, objects, scrambled objects and consonant letter strings. The design contains six 15 second blocks per category, with 16 fast events in each block. The fMRI data were collected using a 1.5 T Siemens scanner. A repetition time of 3 seconds was used and a total of 165 volumes

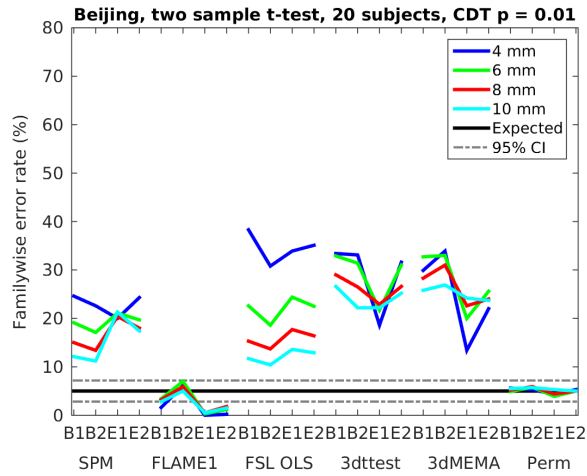
were collected for each run, the spatial resolution is $3 \times 3 \times 3 \text{ mm}^3$ (resulting in volumes of $64 \times 64 \times 35$ voxels). The dataset contains two runs per subject, but only the first run was used in our analysis. The data were analyzed using four regressors; words, objects, scrambled objects, consonant strings. A total of six contrasts were applied; words, objects, scrambled objects, consonant strings, objects versus scrambled objects (0,1,-1,0) and words versus consonant strings (1,0,0,-1). For a cluster defining threshold of $p = 0.01$, a t-threshold of 2.38 was used. For a cluster defining threshold of $p = 0.001$, a t-threshold of 3.28 was used.

Human connectome project

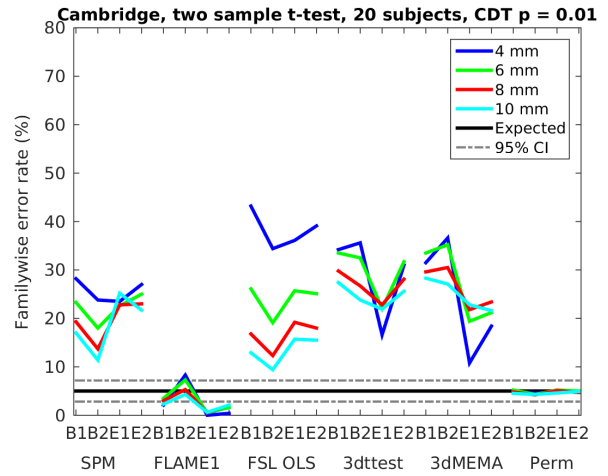
We undertook a follow-up study to understand the conservative results in FSL's FLAME1. FLAME1 estimates the between-subject variance as a positive quantity; while this is natural, if the true between-subject variance is zero, an imperfect (i.e. non-zero) estimation will induce a positive bias and attenuate Z values. The resting fMRI data should have between-subject variance of zero, while task data usually would have a non-zero between-subject variance. To assess FLAME1 under more typical but still null settings, we created randomized two-group studies on *task* fMRI data; a homogeneous group of subjects were split into two equal groups, meaning that the null of equal group activation is true, but there is activation present in the data and likely appreciable between-subject variance.

Specifically, task based fMRI data were downloaded from the human connectome project (HCP, <http://www.humanconnectome.org/>, "Unrelated 80"), to investigate the degree of false positives using task data. fMRI data from 80 unrelated healthy subjects (36 male, age range 22 - 36 years) were downloaded. A total of 7 task datasets were used for all subjects (working memory, gambling, motor, language, social cognition, relational processing, emotion processing), resulting in a total of 87 task contrasts. The fMRI data were collected using a 3 T Siemens Connectome Skyra scanner, with a multiband gradient echo EPI sequence. A repetition time of 0.72 seconds was used, and the spatial resolution is $2 \times 2 \times 2 \text{ mm}^3$ (resulting in volumes of $104 \times 90 \times 72$ voxels). See the HCP website for information about the tasks; <http://www.humanconnectome.org/documentation/Q1/task-fMRI-protocol-details.html>.

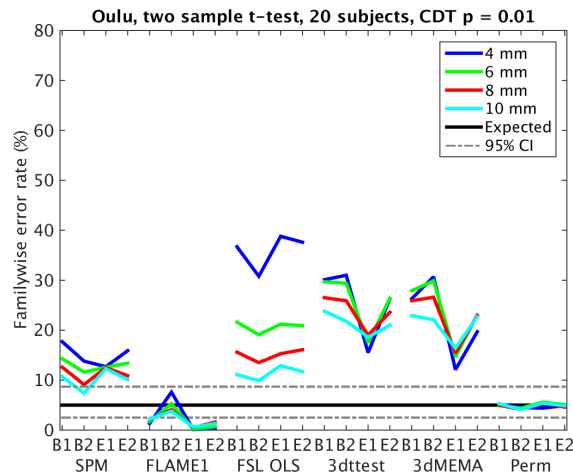
For each of the 87 contrasts, a two sample t-test was applied to a random split of the 80 subjects into two groups of 40 subjects. Each contrast resulting in a significant group difference ($p < 0.05$, FWE cluster corrected) was then counted as a false positive.



(a)

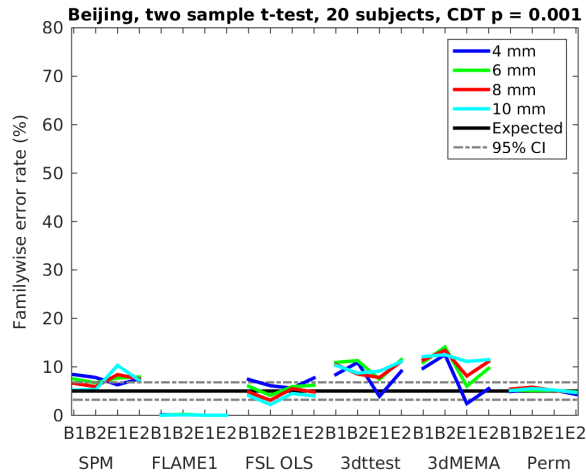


(b)

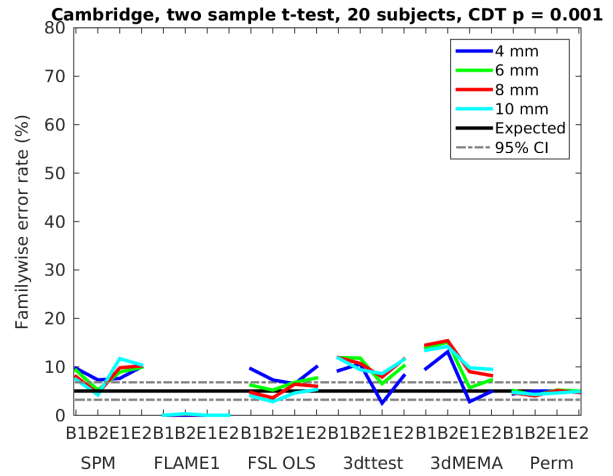


(c)

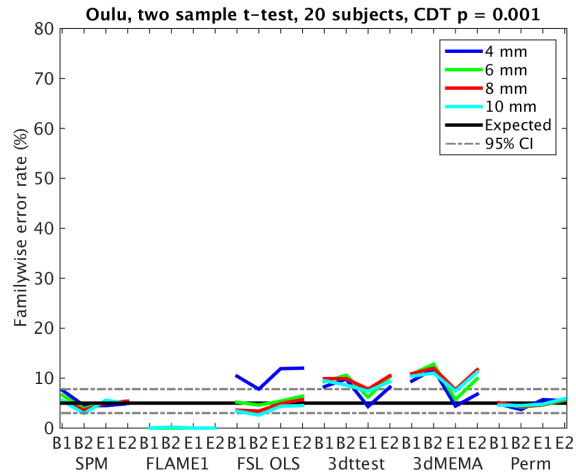
Supplementary Figure 1: Results for two sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.01$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 10 (giving a total of 20 subjects). Each statistic map was first thresholded using a CDT of $p = 0.01$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group differences divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

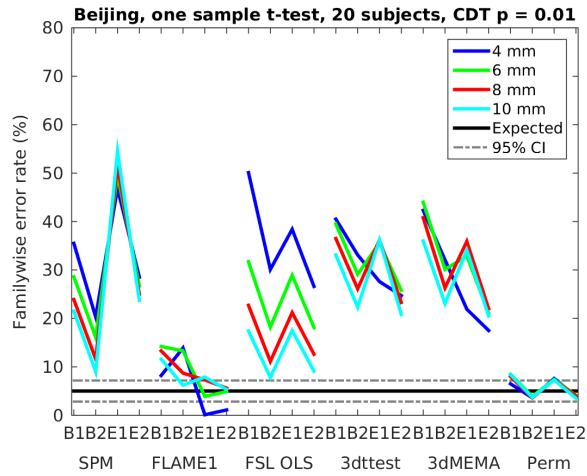


(b)

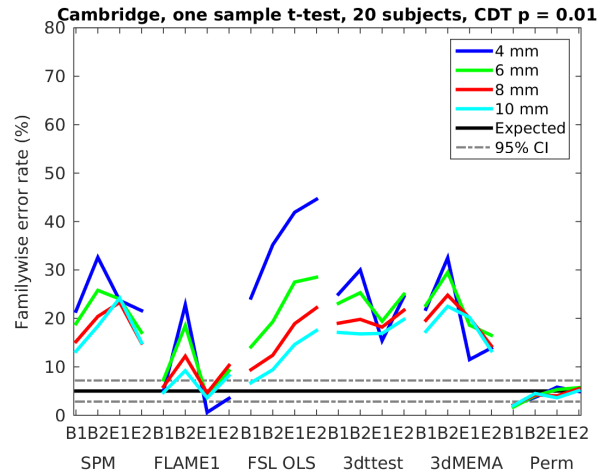


(c)

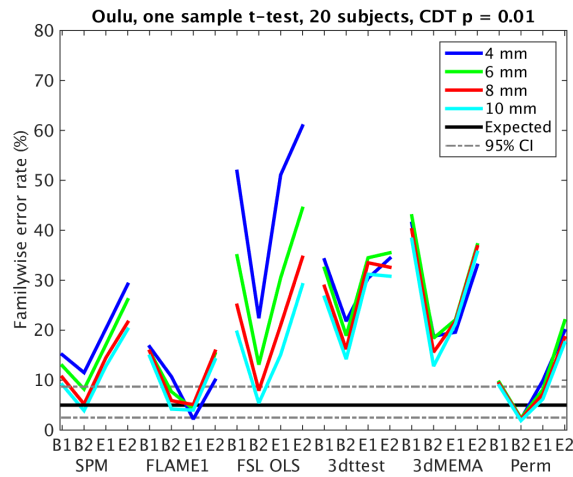
Supplementary Figure 2: Results for two sample *t*-test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.001$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 10 (giving a total of 20 subjects). Each statistic map was first thresholded using a CDT of $p = 0.001$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group differences divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

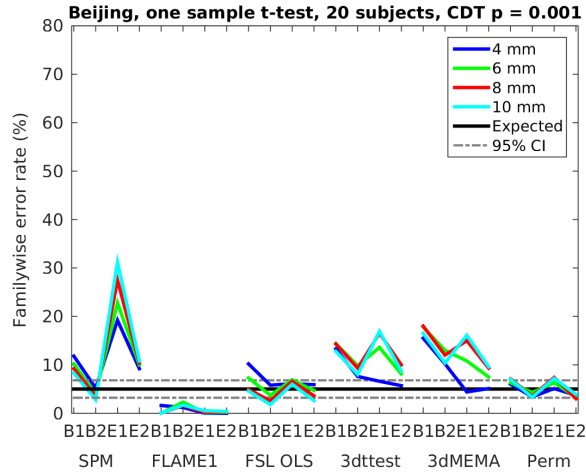


(b)

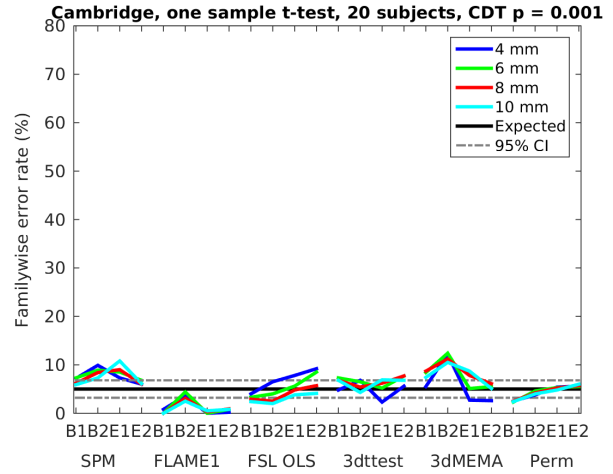


(c)

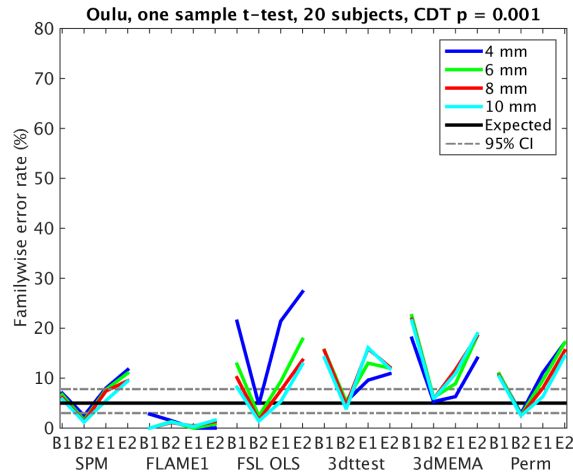
Supplementary Figure 3: Results for one sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.01$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20. Each statistic map was first thresholded using a CDT of $p = 0.01$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group activations divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

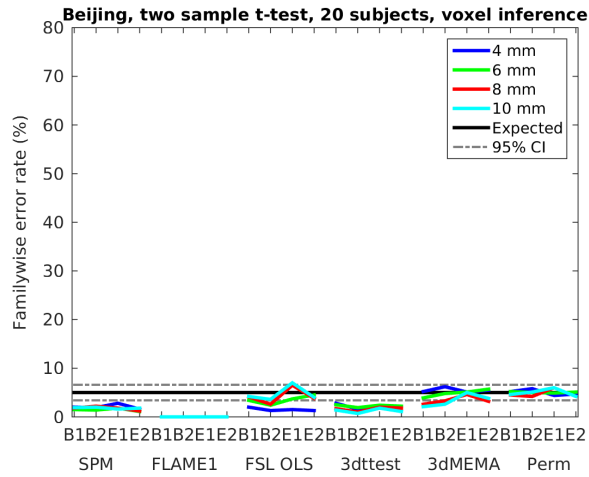


(b)

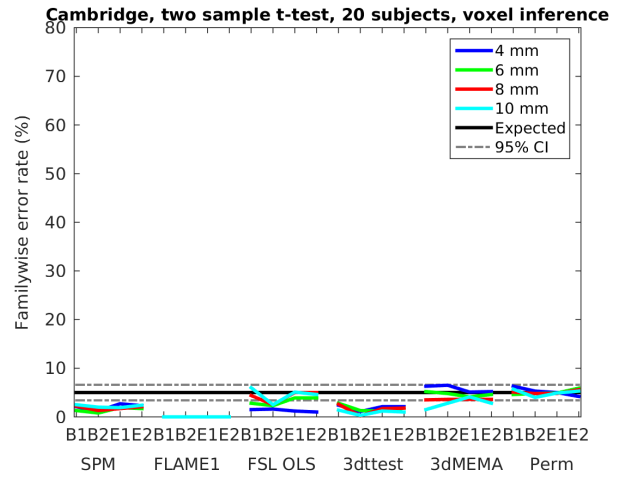


(c)

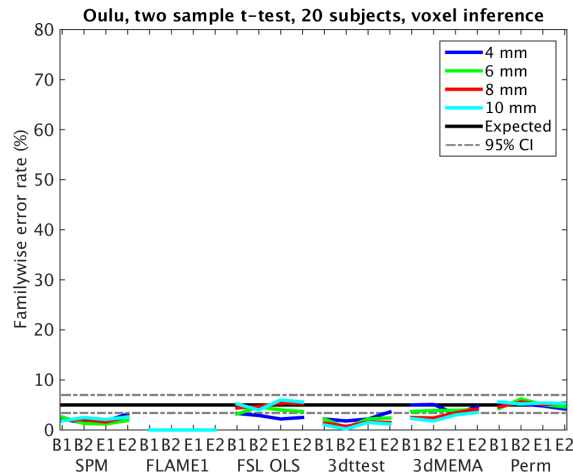
Supplementary Figure 4: Results for one sample *t*-test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.001$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20. Each statistic map was first thresholded using a CDT of $p = 0.001$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group activations divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

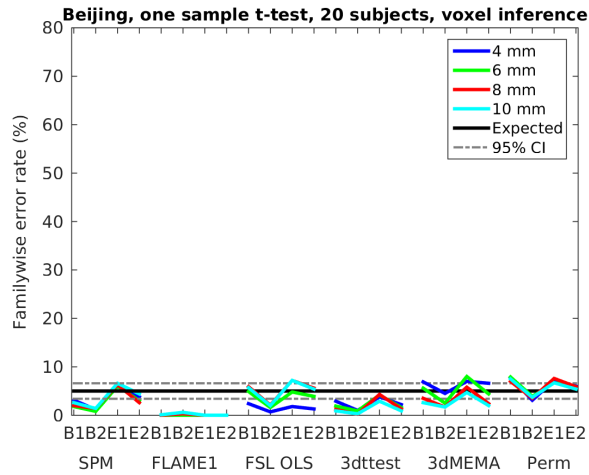


(b)

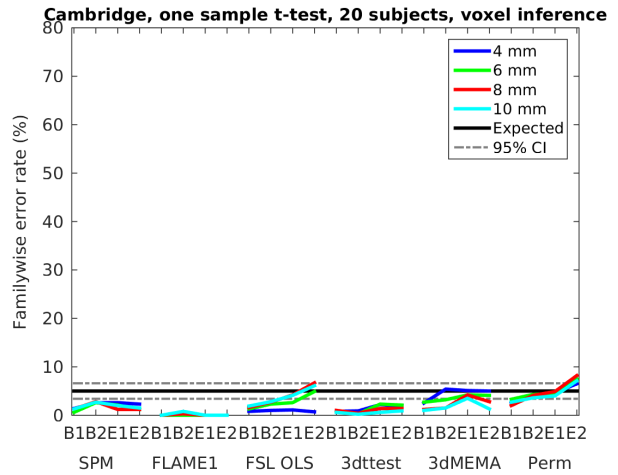


(c)

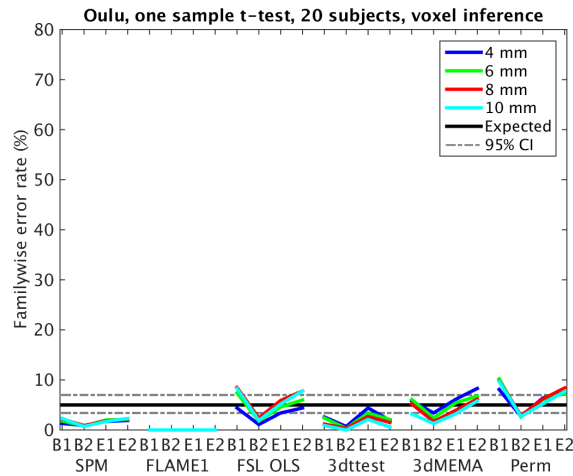
Supplementary Figure 5: Results for two-sample t -test and voxel-wise inference, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 10 (giving a total of 20 subjects). Each statistic map was thresholded using a FWE-corrected voxel-wise threshold of $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant results divided by the number of analyses (1,000). Note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

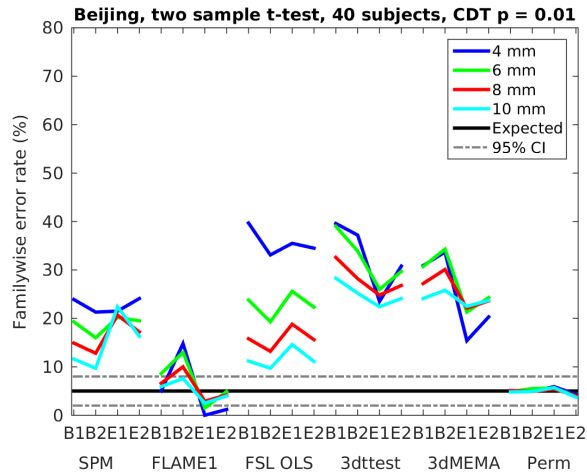


(b)

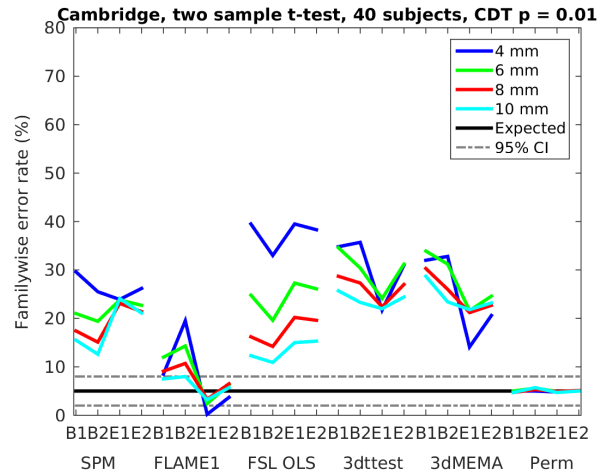


(c)

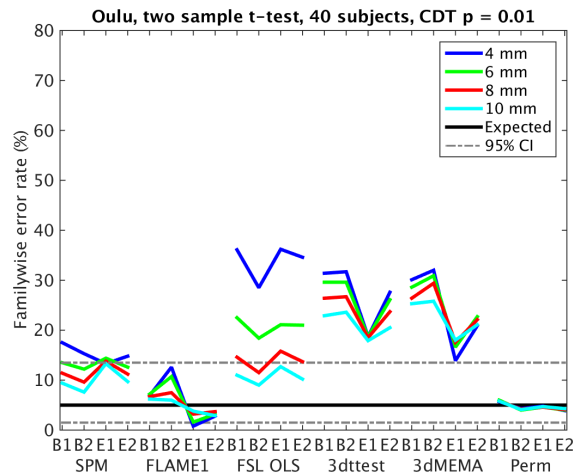
Supplementary Figure 6: Results for one-sample t-test and voxel-wise inference, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20. Each statistic map was thresholded using a FWE-corrected voxel-wise threshold of $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant results divided by the number of analyses (1,000). Note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

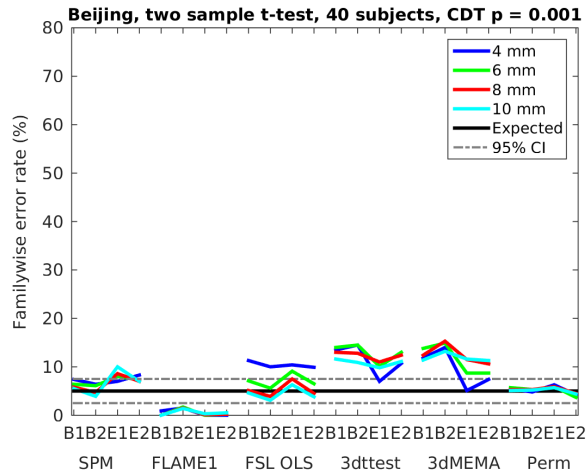


(b)

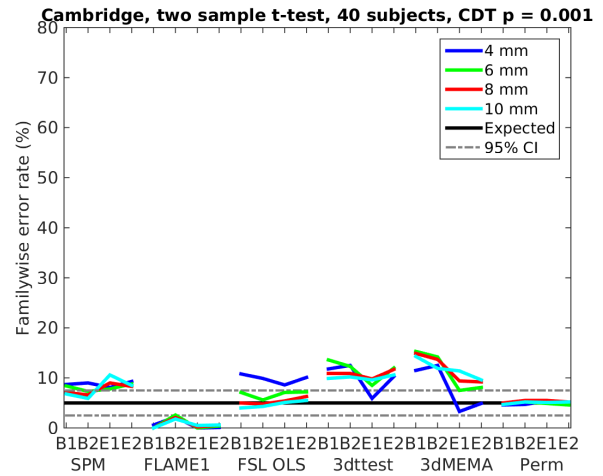


(c)

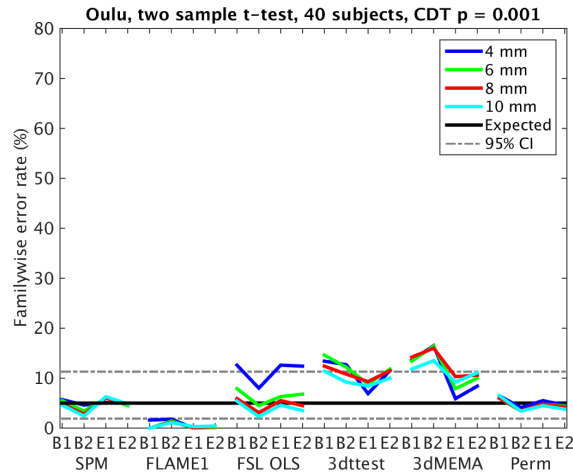
Supplementary Figure 7: Results for two sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.01$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20 (giving a total of 40 subjects). Each statistic map was first thresholded using a CDT of $p = 0.01$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group differences divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

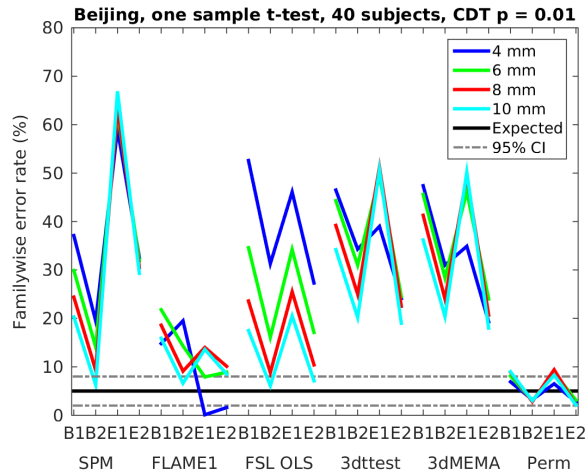


(b)

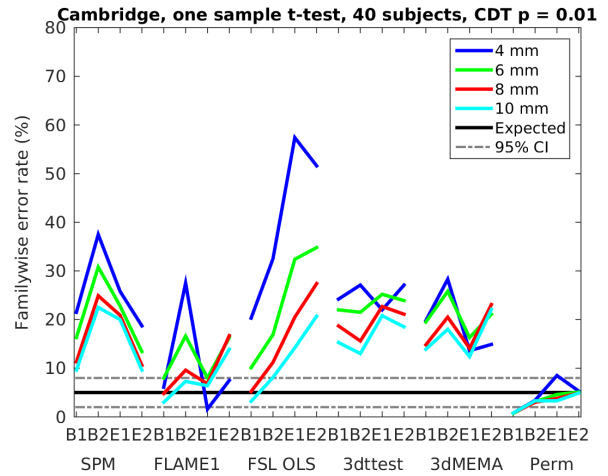


(c)

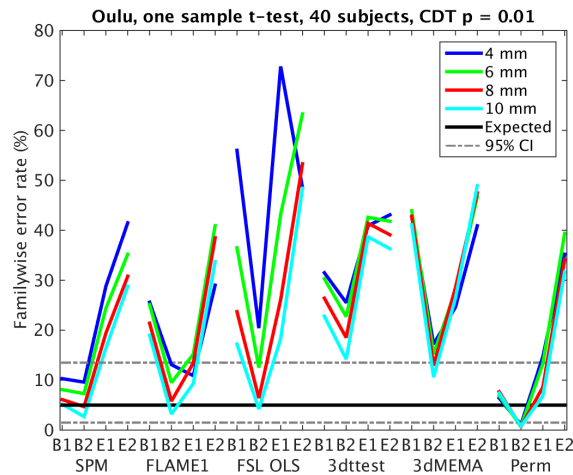
Supplementary Figure 8: Results for two sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.001$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20 (giving a total of 40 subjects). Each statistic map was first thresholded using a CDT of $p = 0.001$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group differences divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

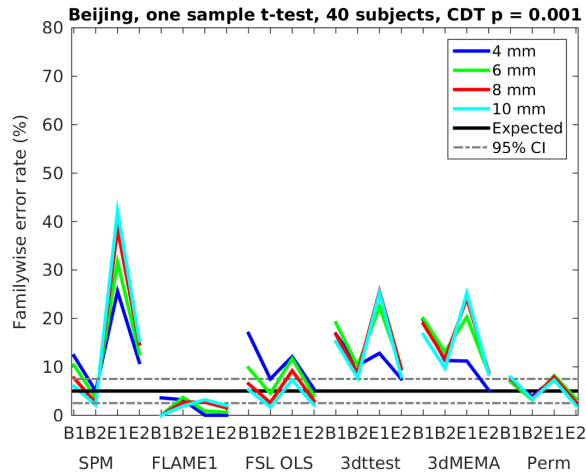


(b)

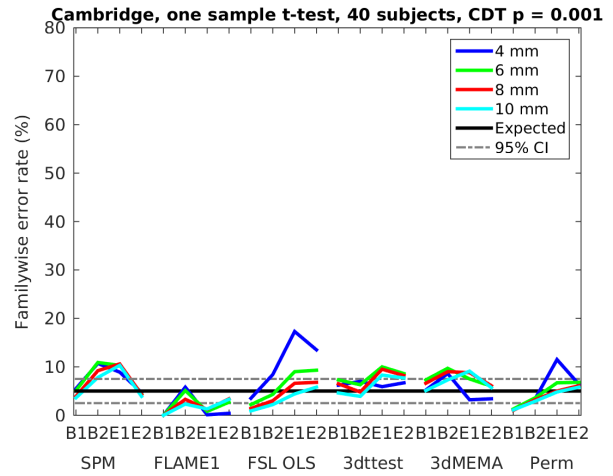


(c)

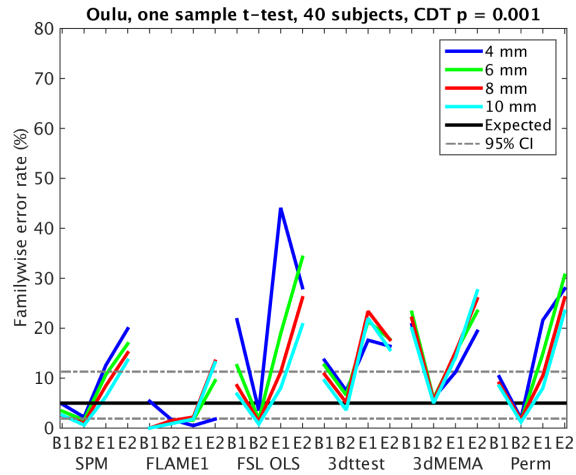
Supplementary Figure 9: Results for one sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.01$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 40. Each statistic map was first thresholded using a CDT of $p = 0.01$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group activations divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

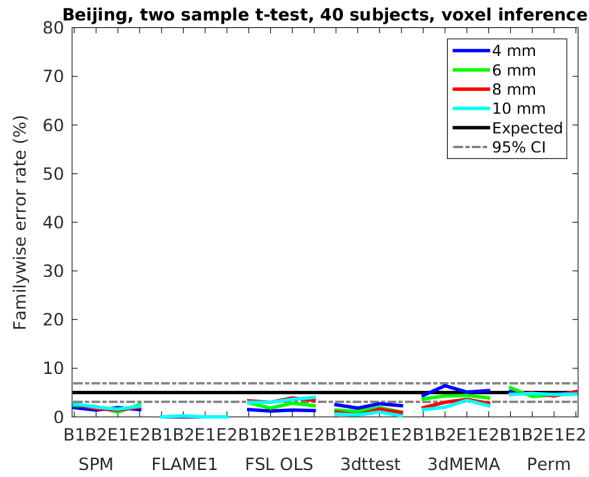


(b)

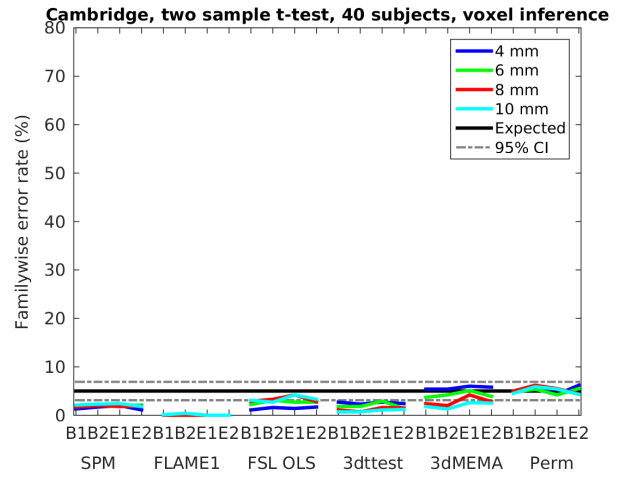


(c)

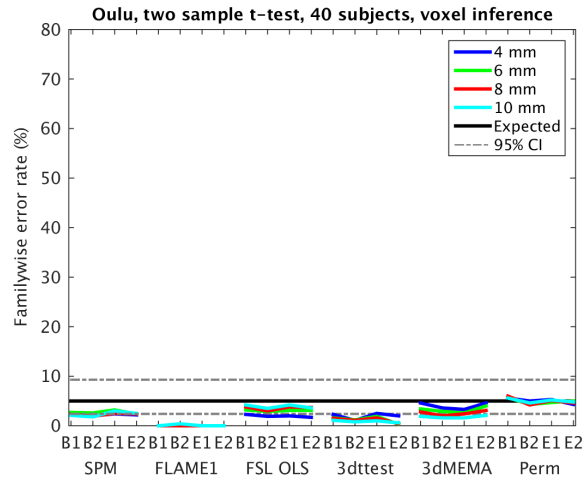
Supplementary Figure 10: Results for one sample t -test and cluster-wise inference using a cluster defining threshold (CDT) of $p = 0.001$, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 40. Each statistic map was first thresholded using a CDT of $p = 0.001$, uncorrected for multiple comparisons, and the surviving clusters were then compared to a FWE-corrected cluster extent threshold, $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant group activations divided by the number of analyses (1,000). Note that the default CDT is $p = 0.001$ in SPM and $p = 0.01$ in FSL (AFNI does not have a default setting). Also note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

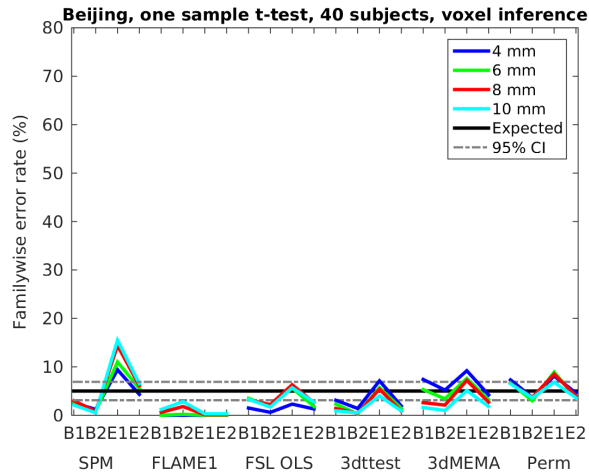


(b)

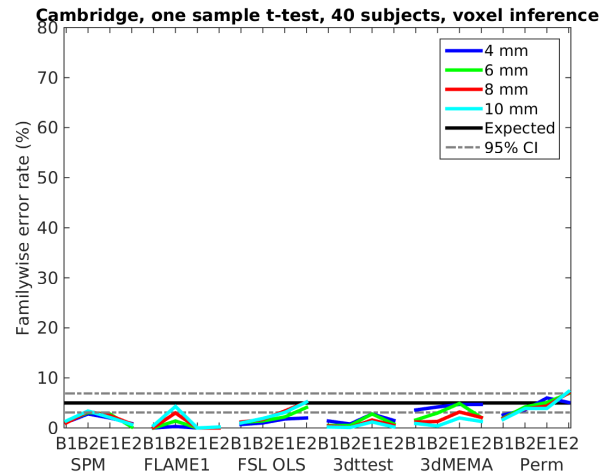


(c)

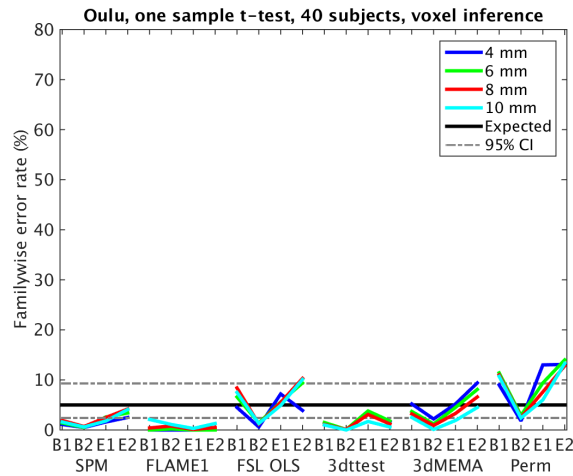
Supplementary Figure 11: Results for two-sample t -test and voxel-wise inference, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 20 (giving a total of 40 subjects). Each statistic map was thresholded using a FWE-corrected voxel-wise threshold of $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant results divided by the number of analyses (1,000). Note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

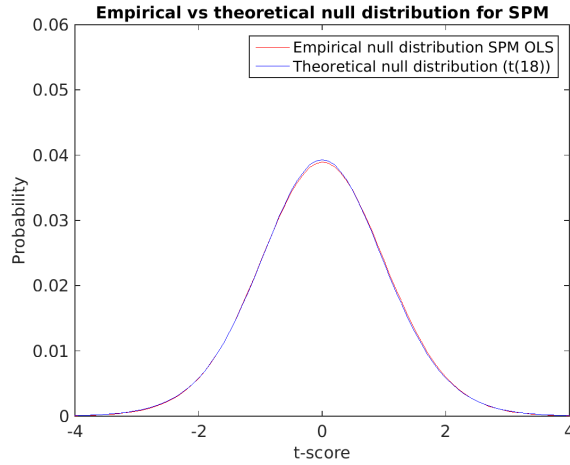


(b)

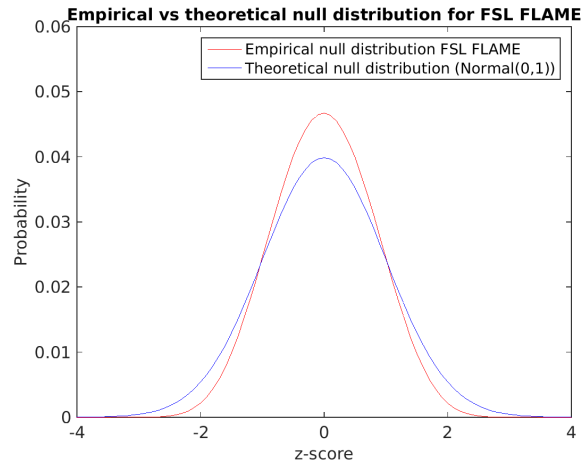
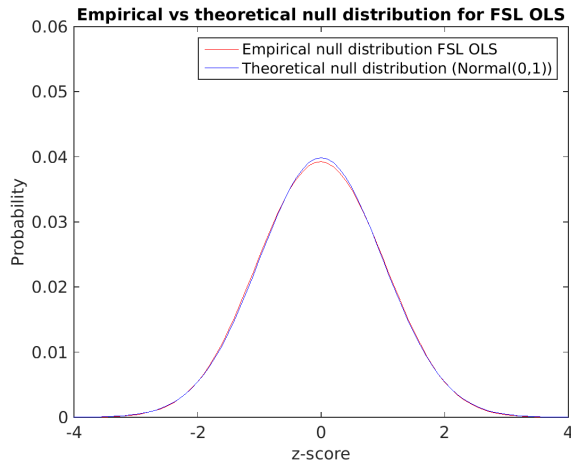


(c)

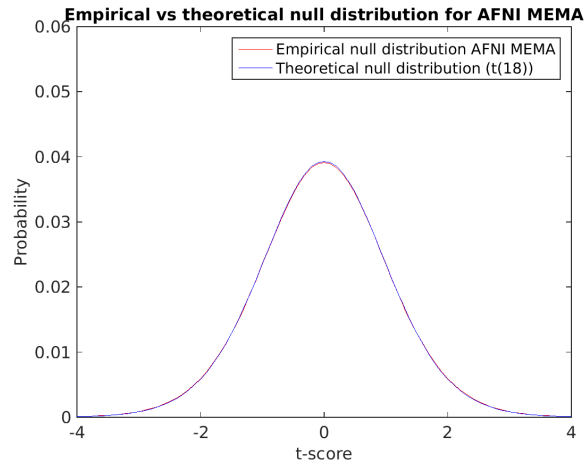
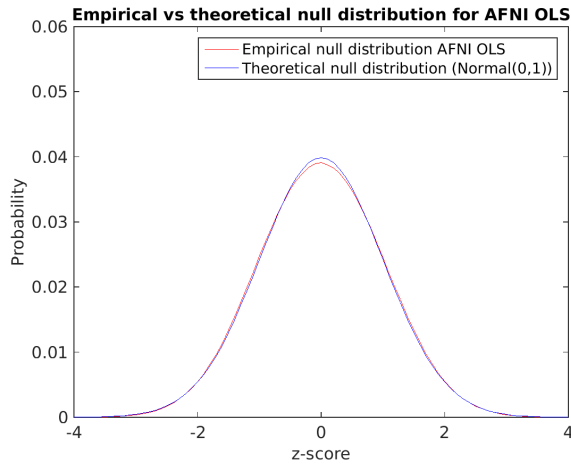
Supplementary Figure 12: Results for one-sample *t*-test and voxel-wise inference, showing estimated familywise error rates for 4 - 10 mm of smoothing and four different activity paradigms (B1, B2, E1, E2), for SPM, FSL, AFNI and a permutation test. These results are for a group size of 40. Each statistic map was thresholded using a FWE-corrected voxel-wise threshold of $p_{FWE} = 0.05$. The estimated familywise error rates are simply the number of analyses with any significant results divided by the number of analyses (1,000). Note that the default amount of smoothing is 8 mm in SPM, 5 mm in FSL and 4 mm in AFNI. (a) results for Beijing data (b) results for Cambridge data (c) results for Oulu data.



(a)

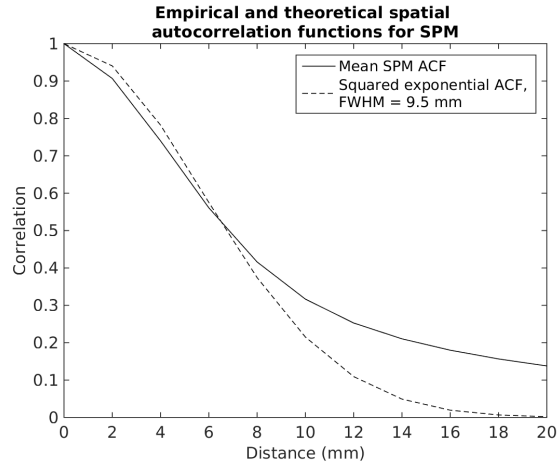


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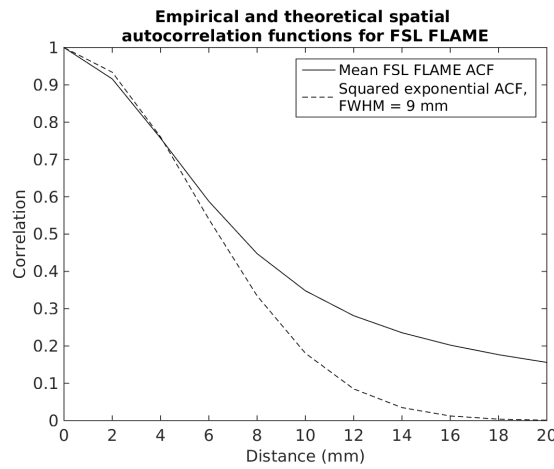
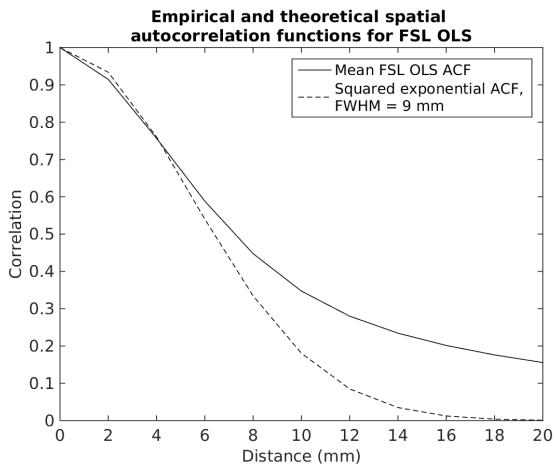


(c)

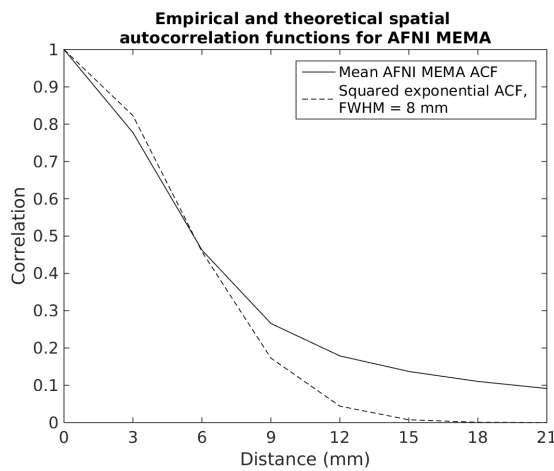
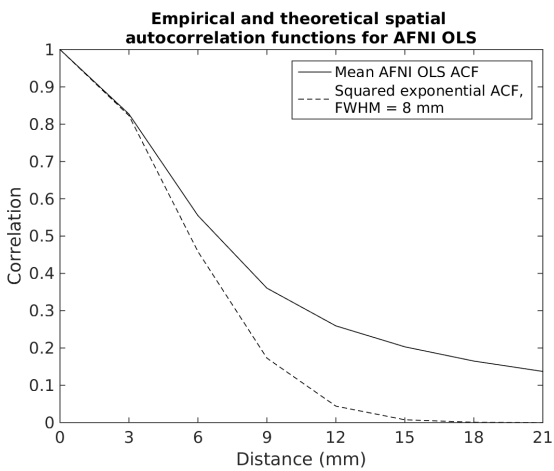
Supplementary Figure 13: Empirical versus theoretical null distributions for a) SPM, b) FSL and c) AFNI. The empirical null distributions were estimated by pooling test values over all brain voxels for 1,000 random group comparisons. The test values were drawn from two sample t-tests (10 subjects per group) using the Beijing data (analyzed with the E2 paradigm and 6 mm smoothing). Note that the empirical null distribution for FLAME1 in FSL has a much lower variance (0.67) compared to a normal distribution with unit variance. For this reason, the familywise error rates are much lower for FLAME in FSL, compared to the other functions.



(a)

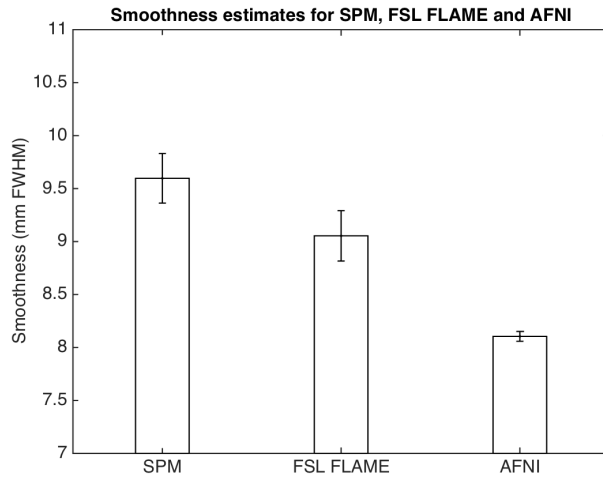


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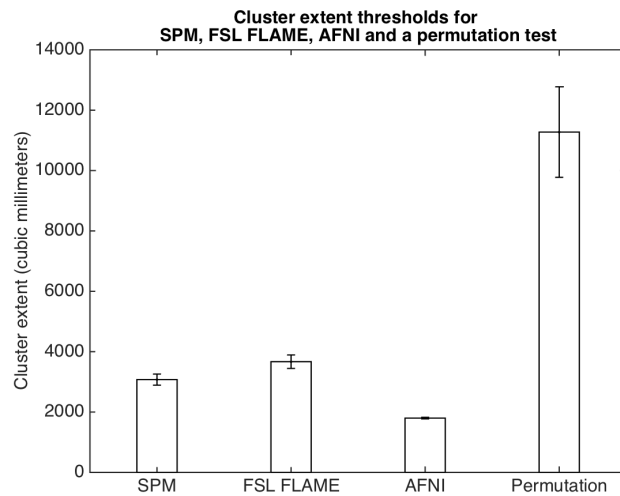


(c)

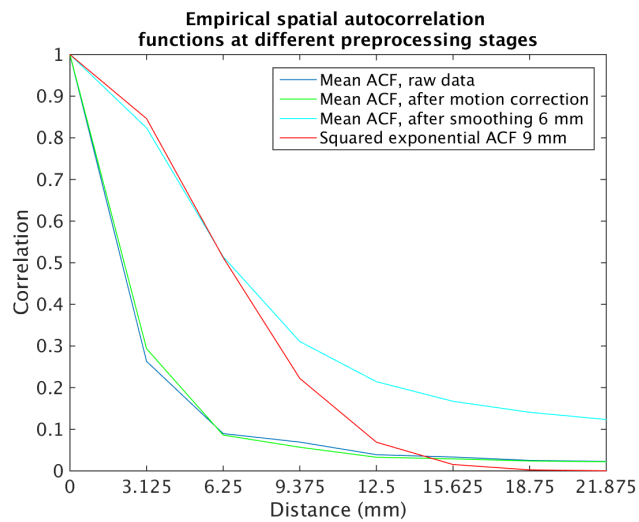
Supplementary Figure 14: Empirical versus theoretical spatial autocorrelation functions (SACFs) for a) SPM, b) FSL and c) AFNI. The SACFs were estimated and averaged using 1,000 group difference maps, generated from two sample *t*-tests (10 subjects per group) using the Beijing data (analyzed with the E2 paradigm and 6 mm smoothing). Note that the empirical SACFs have a much longer tail compared to the theoretical squared exponential SACF, thereby violating one of the required assumptions for parametric cluster-wise inference using Gaussian random field theory. Both SPM and FSL resample the fMRI data to a resolution of 2 mm, while AFNI instead uses a resolution of 3 mm for the specific datasets. For this reason, the SACFs are sampled differently for AFNI.



Supplementary Figure 15: Group smoothness estimates (mm full width at half maximum) for SPM, FSL FLAME and AFNI. The smoothness estimates originate from 1,000 two sample *t*-tests (10 subjects per group) using the Beijing data (analyzed with the E2 paradigm and 6 mm smoothing). Note that AFNI estimates the group smoothness differently compared to SPM and FSL. Also note that AFNI uses higher order interpolation for motion correction and spatial normalization, which leads to a lower smoothness compared to more common linear interpolation. The error bars represent the standard deviation.

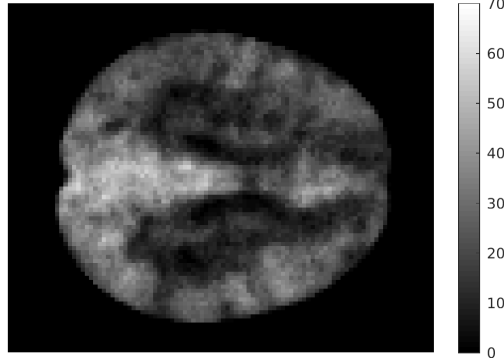


Supplementary Figure 16: Cluster extent thresholds (in cubic millimeters) for SPM, FSL FLAME, AFNI and a permutation test, for a cluster defining threshold of $p = 0.01$ and a familywise cluster error rate of $p = 0.05$. The thresholds originate from 1,000 two sample *t*-tests (10 subjects per group) using the Beijing data (analyzed with the E2 paradigm and 6 mm smoothing). Note that the permutation threshold can only be directly compared with the threshold from the FSL software, as first level results from FSL were used for the non-parametric analyses. The error bars represent the standard deviation.



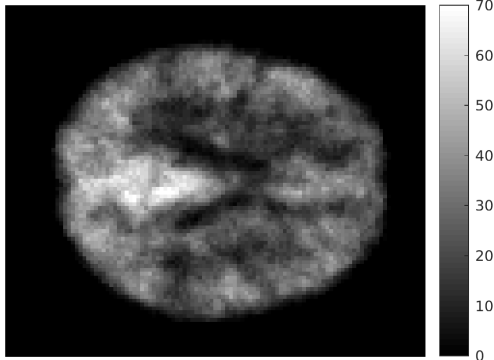
Supplementary Figure 17: *Spatial autocorrelation functions (SACFs) for raw fMRI data, fMRI data after motion correction and fMRI data after motion correction and 6 mm smoothing. A theoretical squared exponential is included as reference. The SACFs were estimated and averaged using the 198 subjects in the Beijing dataset. Note that the long tail exists for the SACF of the raw data. These long tails have also been observed in data collected with an MR phantom [13], indicating that it is a scanner artifact.*

Spatial distribution of false clusters for SPM

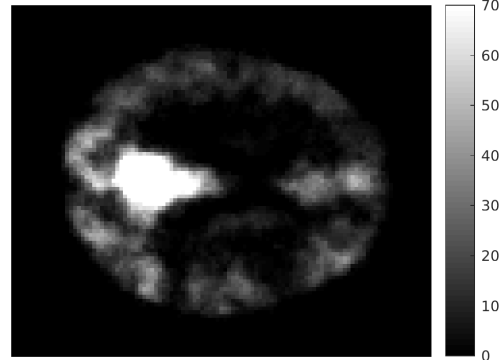


(a)

Spatial distribution of false clusters for FSL OLS

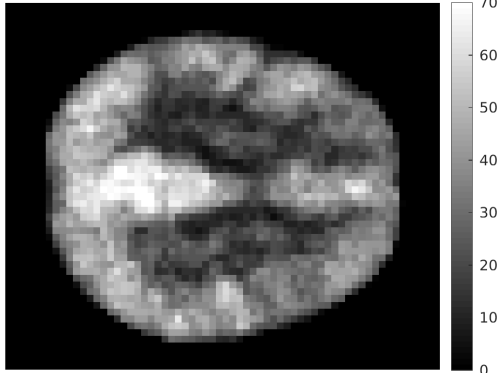


Spatial distribution of false clusters for FSL FLAME

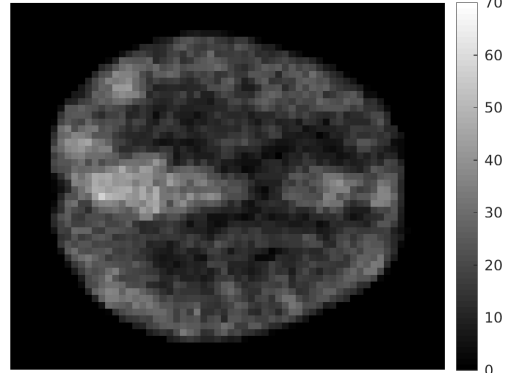


(b)

Spatial distribution of false clusters for AFNI OLS

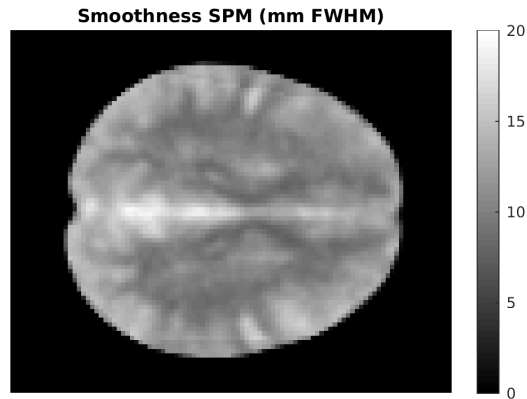


Spatial distribution of false clusters for AFNI MEMA

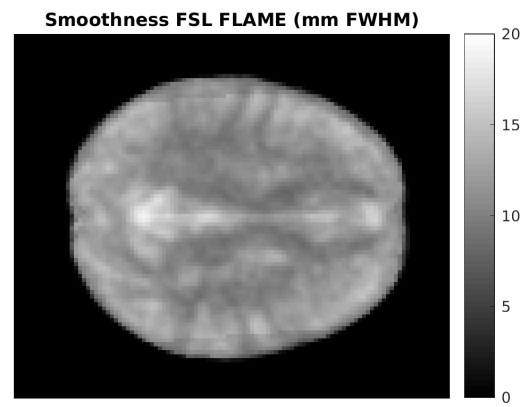
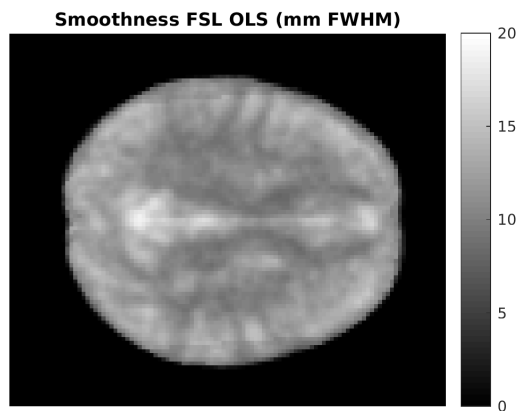


(c)

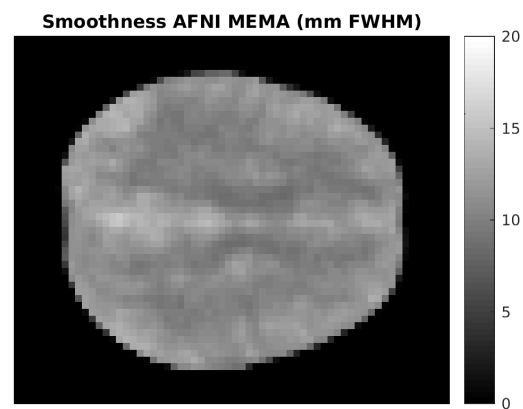
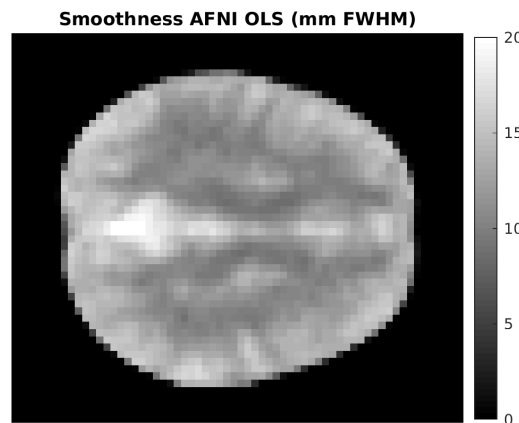
Supplementary Figure 18: *The maps show voxel-wise incidence of false clusters. Image intensity is the number of times, out of 10,000 random analyses (200,000 for FSL FLAME, to account for fewer clusters per analysis), a significant cluster occurred at a given voxel (CDT $p = 0.01$), for a) SPM, b) FSL and c) AFNI. Each analysis is a two sample t -test (10 subjects per group) using the Beijing data, analyzed with the E2 paradigm and 6 mm smoothing. The bright spot in the posterior cingulate corresponds to a region of high smoothness, and suggests non-stationarity as a possible contributing factor.*



(a)

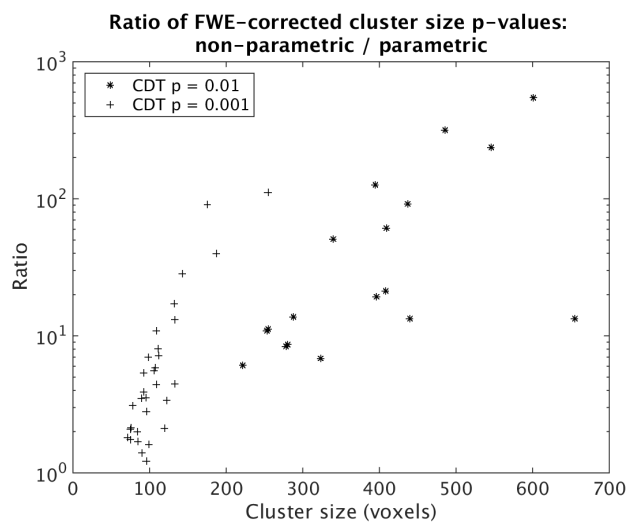


(b)

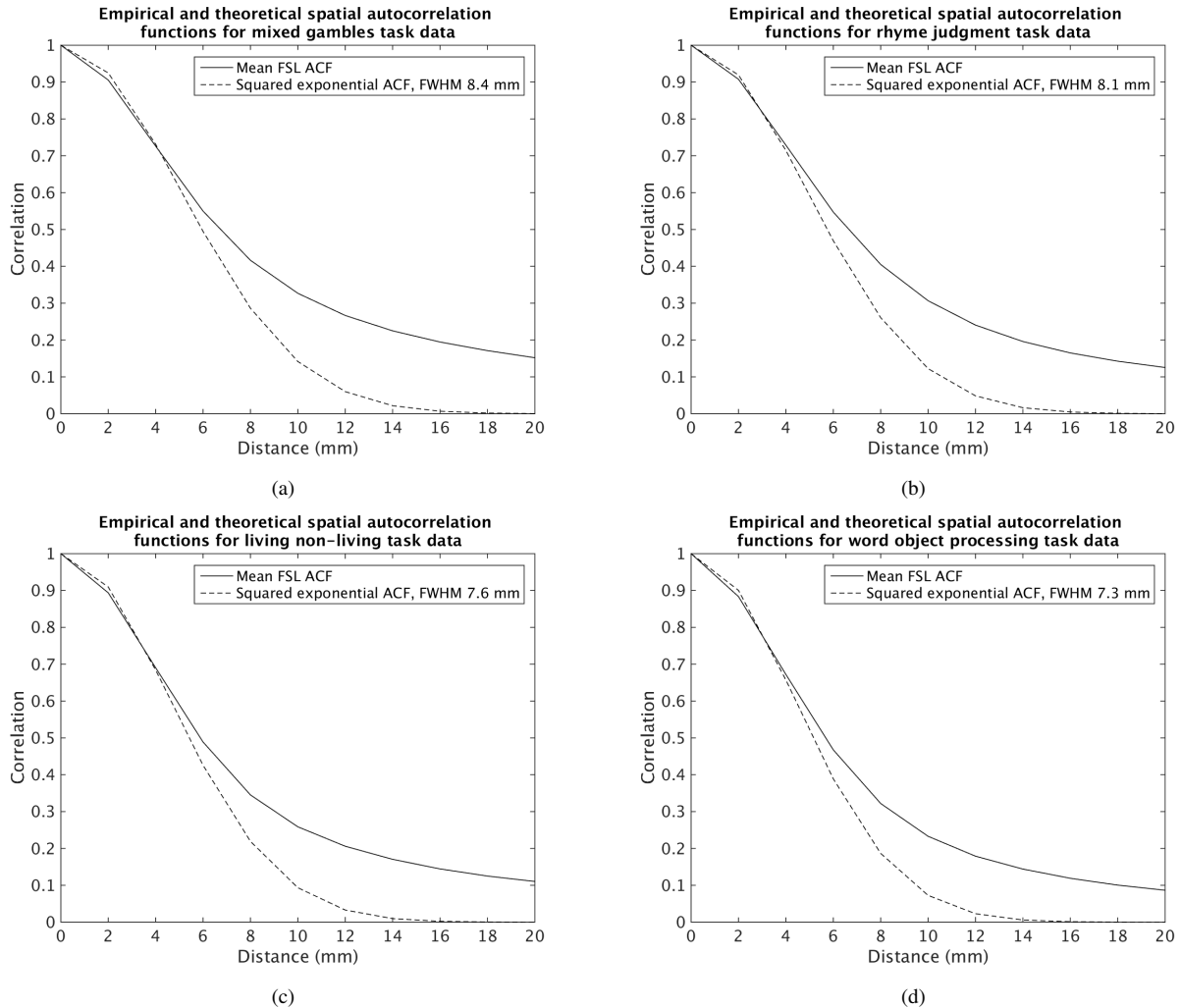


(c)

Supplementary Figure 19: Maps of voxel-wise smoothness for a) SPM, b) FSL and c) AFNI. The smoothness was estimated and averaged using 1,000 group residuals, generated from two sample t-tests (10 subjects per group) using the Beijing data (analyzed with the E2 paradigm and 6 mm smoothing). It is clear that the smoothness varies spatially; one of the required assumptions for parametric cluster-wise inference using Gaussian random field theory is thereby violated. Note that the bright areas (high smoothness) match the spatial maps of the false clusters; it is more likely to find a large cluster for areas with a high smoothness. Note the reduced smoothness for the iterative method AFNI 3dMEMA compared to the corresponding non-iterative method AFNI OLS; the voxel-by-voxel estimation of between subject variance in the iterative methods reduces the smoothness slightly.



Supplementary Figure 20: Ratio of non-parametric to parametric FWE corrected p -values for cluster size inference on 4 task (non-null) fMRI datasets, for parametric FWE p -values $0.05 \geq p \geq 10^{-4}$. Results for two CDT are shown, $p = 0.01$ and $p = 0.001$, and larger ratios indicate parametric p -values being smaller (more significant) than non-parametric p -values (note the logarithmic scale on the y-axis). Clusters with a parametric FWE p -value more significant than 10^{-4} are excluded because a permutation test with 5000 permutations can only resolve p -values down to 0.0002, and such p -values would generate large ratios inherently. These results suggest cluster size inference with a CDT of $p = 0.01$ has FWE inflated by 2 to almost 3 orders of magnitude, and a CDT of $p = 0.001$ has FWE significance inflated by up to 2 orders of magnitude.



Supplementary Figure 21: Empirical versus theoretical spatial autocorrelation functions (SACFs) for the four task datasets; a) mixed-gambles b) rhyme judgment c) living-nonliving decision with plain or mirror-reversed text d) word and object processing. The SACFs were estimated using the group residuals from each group analysis. The fMRI data for each subject were analyzed in FSL, using 5 mm of smoothing (FSL default). Note that the empirical SACFs have a much longer tail compared to the theoretical squared exponential SACF, thereby violating one of the required assumptions for parametric cluster-wise inference using Gaussian random field theory.

Supplementary Table 2: Estimated familywise error rates (FWE) for parametric stationary and non-stationary cluster inference. The results are for a two-sample t-test, 10 subjects per group, for data analyzed with the B2 paradigm and 4 mm smoothing.

Dataset	Cluster defining threshold	Stationary FWE	Non-stationary FWE
Beijing	p = 0.01	21.8%	15.8%
Beijing	p = 0.001	7.6%	10.9%
Cambridge	p = 0.01	23.8%	17.6%
Cambridge	p = 0.001	7.9%	10.9%
Oulu	p = 0.01	15.5%	12.5%
Oulu	p = 0.001	6.3%	13.4%

Supplementary Table 3: Cluster FWE p-values for FSL OLS and a permutation test, for 4 fMRI studies comprising a total of 18 contrasts. A cluster defining threshold of $p = 0.01$ ($z = 2.3$) was used, all clusters with FSL OLS FWE $p < 0.05$ are listed. A star denotes that the parametric p-value is below 0.05, while the non-parametric p-value is not. Note that the resolution of the permutation p-values is 0.0002, since 5000 permutations (or sign flips) were used.

OpenfMRI dataset	Subjects	Cluster size (voxels)	FSL OLS p-value	Perm OLS p-value
Rhyme judgment, contrast 1	13	53877	0	0.0002
Rhyme judgment, contrast 2	13	27484	0	0.0002
		14682	$1.37 \cdot 10^{-40}$	0.002
		3467	$1.16 \cdot 10^{-14}$	0.024
Rhyme judgment, contrast 3	13	799	$4.8 \cdot 10^{-5}$	0.097 *
		408	0.0103	0.219 *
Rhyme judgment, contrast 4	13	No surviving clusters		
Mixed gambles, contrast 1	16	13284	$1.36 \cdot 10^{-36}$	0.005
		440	0.0152	0.202 *
Mixed gambles, contrast 2	16	No surviving clusters		
Mixed gambles, contrast 3	16	No surviving clusters		
Mixed gambles, contrast 4	16	655	0.00888	0.118 *
Living-nonliving decision, contrast 1	14	8612	$3.46 \cdot 10^{-33}$	0.001
		7577	$2.37 \cdot 10^{-30}$	0.002
		5920	$1.6 \cdot 10^{-25}$	0.003
		1439	$4.88 \cdot 10^{-9}$	0.035
		601	0.000213	0.116 *
Living-nonliving decision, contrast 2	14	751	$2.75 \cdot 10^{-5}$	0.08 *
		669	$8.71 \cdot 10^{-5}$	0.096 *
		546	0.000541	0.128 *
Living-nonliving decision, contrast 3	14	396	0.00889	0.172 *
		323	0.0302	0.207 *
Living-nonliving decision, contrast 4	14	No surviving clusters		
Word and object processing, contrast 1	49	7397	$2.3 \cdot 10^{-32}$	0.001
		6586	$7.57 \cdot 10^{-30}$	0.001
		6232	$1.02 \cdot 10^{-28}$	0.002
		2834	$2.11 \cdot 10^{-16}$	0.01
		486	0.00044	0.139 *
		288	0.0182	0.249 *
Word and object processing, contrast 2	49	7062	$9.77 \cdot 10^{-30}$	0.001
		6158	$5.08 \cdot 10^{-27}$	0.002
		5529	$4.73 \cdot 10^{-25}$	0.003
		1853	$2.27 \cdot 10^{-11}$	0.025
		1523	$8.3 \cdot 10^{-10}$	0.035
		1465	$1.6 \cdot 10^{-9}$	0.037
		1382	$4.18 \cdot 10^{-9}$	0.04
		437	0.00174	0.159 *
		409	0.00283	0.173 *
Word and object processing, contrast 3	49	42205	0	0.0002
		998	$1.79 \cdot 10^{-7}$	0.054 *
Word and object processing, contrast 4	49	32404	0	0.0002
		12837	$2.8 \cdot 10^{-45}$	0.001
		280	0.0287	0.248 *
		278	0.0299	0.251 *
Word and object processing, contrast 5	49	2118	$3.05 \cdot 10^{-14}$	0.017
		881	$2.98 \cdot 10^{-7}$	0.051 *
		395	0.00115	0.146 *
		340	0.00354	0.18 *
		255	0.0226	0.253 *
		253	0.0237	0.258 *
		222	0.0486	0.297 *
Word and object processing, contrast 6	49	27767	0	0.0002
		6183	$9.65 \cdot 10^{-29}$	0.005

Supplementary Table 4: Cluster FWE p-values for FSL OLS and a permutation test, for 4 fMRI studies comprising a total of 18 contrasts. A cluster defining threshold of $p = 0.001$ ($z = 3.1$) was used, all clusters with FSL OLS FWE $p < 0.05$ are listed. A star denotes that the parametric p-value is below 0.05, while the non-parametric p-value is not. Note that the resolution of the permutation p-values is 0.0002, since 5000 permutations (or sign flips) were used.

OpenfMRI dataset	Subjects	Cluster size (voxels)	FSL OLS p-value	Perm OLS p-value
Rhyme judgment, contrast 1	13	13877	0	0.0002
		4859	$1.18 \cdot 10^{-38}$	0.001
		2273	$5.44 \cdot 10^{-23}$	0.002
		2039	$2.49 \cdot 10^{-21}$	0.002
		1081	$1.04 \cdot 10^{-13}$	0.005
		473	$1.19 \cdot 10^{-7}$	0.008
		306	$1.78 \cdot 10^{-5}$	0.011
		133	0.00806	0.038
		122	0.0127	0.042
		99	0.0347	0.055 *
Rhyme judgment, contrast 2	13	14470	0	0.0002
		3074	$5.43 \cdot 10^{-27}$	0.001
		1868	$3.7 \cdot 10^{-19}$	0.002
		1558	$6.83 \cdot 10^{-17}$	0.002
		874	$2.95 \cdot 10^{-11}$	0.004
		422	$1.19 \cdot 10^{-6}$	0.008
		255	0.000153	0.014
96	0.0498	0.06 *		
Rhyme judgment, contrast 3	13	No surviving clusters		
Rhyme judgment, contrast 4	13	No surviving clusters		
Mixed gambles, contrast 1	16	766	$7.01 \cdot 10^{-10}$	0.001
		120	0.0237	0.053 *
Mixed gambles, contrast 2	16	No surviving clusters		
Mixed gambles, contrast 3	16	No surviving clusters		
Mixed gambles, contrast 4	16	No surviving clusters		
Living-nonliving decision, contrast 1	14	3310	$1.69 \cdot 10^{-33}$	0.0002
		1901	$6.95 \cdot 10^{-23}$	0.0002
		761	$4.8 \cdot 10^{-12}$	0.001
		569	$8.96 \cdot 10^{-10}$	0.002
		417	$5.96 \cdot 10^{-8}$	0.002
		187	0.000326	0.013
		109	0.0109	0.038
		96	0.021	0.047
		85	0.0373	0.06 *
		84	0.0394	0.061 *
		90	0.0301	0.046
Living-nonliving decision, contrast 2	14	No surviving clusters		
Living-nonliving decision, contrast 3	14	No surviving clusters		
Living-nonliving decision, contrast 4	14	No surviving clusters		

Supplementary Table 5: Cluster FWE p-values for FSL OLS and a permutation test, for 4 fMRI studies comprising a total of 18 contrasts. A cluster defining threshold of $p = 0.001$ ($z = 3.1$) was used, all clusters with FSL OLS FWE $p < 0.05$ are listed. A star denotes that the parametric p-value is below 0.05, while the non-parametric p-value is not. Note that the resolution of the permutation p-values is 0.0002, since 5000 permutations (or sign flips) were used.

OpenfMRI dataset	Subjects	Cluster size (voxels)	FSL OLS p-value	Perm OLS p-value
Word and object processing, contrast 1	49	4644	$1.4 \cdot 10^{-45}$	0.0002
		4017	$2.35 \cdot 10^{-41}$	0.0002
		2615	$7.21 \cdot 10^{-31}$	0.0002
		828	$6.38 \cdot 10^{-14}$	0.001
		765	$3.64 \cdot 10^{-13}$	0.001
		543	$2.57 \cdot 10^{-10}$	0.003
		306	$8.34 \cdot 10^{-7}$	0.006
		292	$1.49 \cdot 10^{-6}$	0.006
		176	0.000187	0.017
Word and object processing, contrast 2	49	5000	$1.4 \cdot 10^{-45}$	0.0002
		3902	$1.61 \cdot 10^{-38}$	0.0002
		1540	$2.22 \cdot 10^{-20}$	0.0002
		1199	$3.92 \cdot 10^{-17}$	0.0002
		1035	$1.84 \cdot 10^{-15}$	0.0002
		989	$5.6 \cdot 10^{-15}$	0.001
		759	$1.96 \cdot 10^{-12}$	0.001
		699	$9.92 \cdot 10^{-12}$	0.001
		497	$3.42 \cdot 10^{-9}$	0.003
		413	$5.96 \cdot 10^{-8}$	0.004
		133	0.00222	0.029
		95	0.0149	0.053 *
		Word and object processing, contrast 3	49	27735
1312	$2.62 \cdot 10^{-19}$			0.001
1264	$8.15 \cdot 10^{-19}$			0.001
789	$1.57 \cdot 10^{-13}$			0.002
525	$3.99 \cdot 10^{-10}$			0.004
415	$1.53 \cdot 10^{-8}$			0.005
209	$4.05 \cdot 10^{-5}$			0.013
143	0.000845			0.024
Word and object processing, contrast 4	49	24890	0	0.0002
		3525	$2.79 \cdot 10^{-36}$	0.0002
		1678	$7.98 \cdot 10^{-22}$	0.0002
		1492	$4.01 \cdot 10^{-20}$	0.001
		996	$3.42 \cdot 10^{-15}$	0.002
		845	$1.55 \cdot 10^{-13}$	0.003
		346	$4.17 \cdot 10^{-7}$	0.008
		112	0.00582	0.042
		107	0.00751	0.044
		106	0.00791	0.044
		75	0.0425	0.074 *
		Word and object processing, contrast 5	49	373
282	$7.75 \cdot 10^{-7}$			0.006
109	0.00302			0.033
98	0.00574			0.04
92	0.00821			0.044
78	0.0195			0.06 *
Word and object processing, contrast 6	49	11134	0	0.0002
		3466	$1.21 \cdot 10^{-37}$	0.001
		1630	$1.87 \cdot 10^{-22}$	0.001
		609	$2.86 \cdot 10^{-11}$	0.003
		475	$1.98 \cdot 10^{-9}$	0.004
		270	$3.16 \cdot 10^{-6}$	0.009
		132	0.00145	0.025
		111	0.00433	0.035
		92	0.0123	0.048
		89	0.0146	0.051 *
		76	0.0313	0.067 *
		75	0.0332	0.069 *

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