

1 **How does the cerebellum contribute to cognitive functions?**

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Abstract

Over the past 70 years, neuroscience has gained a deep understanding of how the cerebellum supports basic motor functions. Anatomical, clinical, and neuroimaging studies, however, have also firmly established that the cerebellum plays an important role in cognition. Even though this topic has received considerable attention, we still do not know the exact nature of this contribution. Here we review known facts about how the cerebellum contributes to cognition and identify roadblocks that have prevented the development of a unified theory. Addressing these key questions should help the field develop testable, falsifiable hypotheses that are needed for solving this intriguing question.

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Main text

50 ***Introduction***

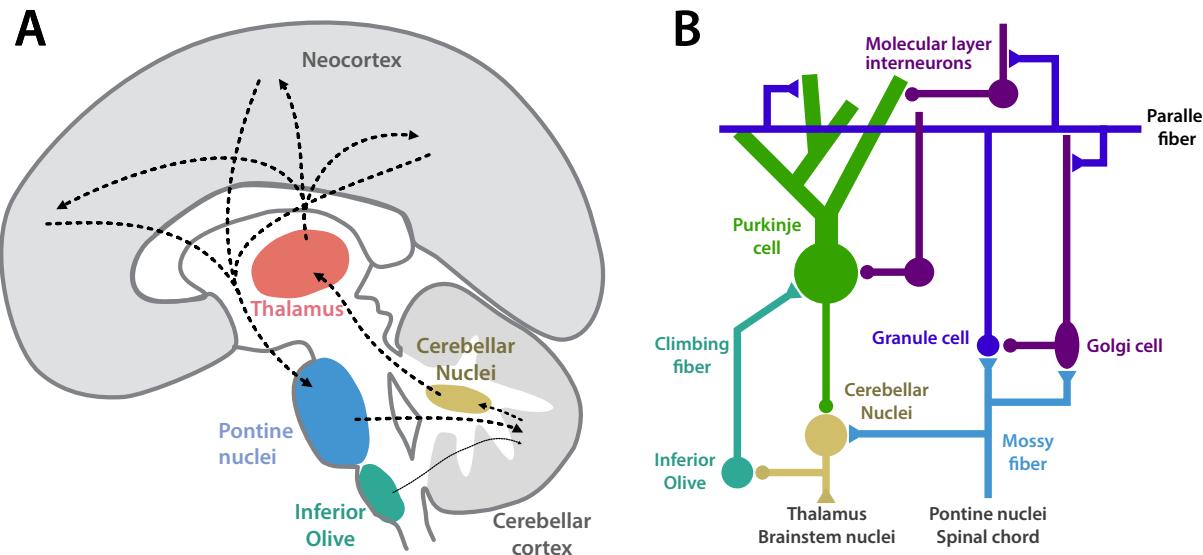
51 The cerebellum is a brain structure full of contradictions. On the one hand, we know a lot about
52 its anatomy, circuitry, and plasticity mechanisms. Indeed, for more than 50 years we have had a
53 compelling theory of how the cerebellum learns, a theory that, in broad strokes, has stood the
54 test of time remarkably well. Despite this wealth of insight, however, we still lack a concise
55 answer to the seemingly simple question: What does the cerebellum actually do?

56 In the human brain, approximately 40 million axons leave the neocortex through the
57 cerebral peduncles [1], and most of these send collaterals to the pontine nuclei, which then give
58 rise to mossy fibers (Fig. 1a). In the cerebellar cortex, these mossy fibers synapse onto 50
59 billion granule cells, which make up more than half the neurons in the human brain [2]. The
60 axons of granule cells, the parallel fibers, then connect to Purkinje cells (Fig. 1b), the output
61 neurons of the cerebellar cortex. In the human, each Purkinje cell receives ~1,000,000 parallel-
62 fiber synapses. Purkinje cells have a high spontaneous firing rate (50-70 Hz) and tonically inhibit
63 the downstream cerebellar nuclei.

64 Purkinje cells are also innervated by one, or sometime two [3] climbing fibers, which
65 originate in the inferior olive and which fire at relatively low rates (0-3Hz). Despite its relative
66 sparseness, the climbing fiber input acts as a strong plasticity signal that modifies parallel-fiber-
67 to-Purkinje cell synapses [4]. This and other plasticity sites create a circuit, in which each
68 Purkinje cell learns to predict its climbing fiber input from the concurrent high-dimensional
69 activity patterns of its parallel fibers. The firing rate of the Purkinje cell then goes down,
70 releasing the inhibition of the deep cerebellar nuclei cells, which then start to fire vigorously. The
71 prediction is usually well-timed, anticipating the climbing fiber input by tens to hundreds of
72 milliseconds. Cells in the cerebellar nuclei then project to the inferior olive, other subcortical
73 nuclei, recurrently back to the cerebellar cortex [5], and, most prevalent in the human, to the
74 neocortex via the thalamus. In summary, the cerebellum looks like a high-capacity learning
75 engine that can provide a precisely timed predictive signal learned from a very high-dimensional
76 input.

This basic idea of how the local cerebellar circuit learns and predicts was formulated by Marr [6], Albus [7], and Ito [8], and has evolved into a well-established theory [9]. Among other functions, this framework can successfully explain many of the basic phenomena seen in cerebellar contributions to sensorimotor tasks like eye-blink conditioning [10], adaptation of the vestibular-ocular reflex, and modulation of smooth-pursuit eye movements [11,12].

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83

84 **Figure 1. (A)** Schematic diagram of the neocortical-cerebellar circuit, with pontine nuclei providing mossy
 85 fiber input, and the inferior olive climbing fiber input to the cerebellar cortex. The output is sent back to the
 86 neocortex via cerebellar nuclei and thalamus. **(B)** Wiring diagram of the local circuitry within the
 87 cerebellum. Excitatory synapses are shown as triangles, inhibitory synapses as circles. We note that for
 88 simplicity this schematic is leaving out additional potentially important connections, such as projections
 89 from the cerebellar nuclei onto granule cells [5,71].

90 **Cerebellar function in cognition**

91 Even though the most salient symptoms of cerebellar damage or degeneration in adulthood are
 92 the disruption of the smooth coordination of movement [13], the majority of the human
 93 cerebellum is likely not concerned with motor control but instead contributes to a wide range of
 94 cognitive functions. Leiner, Leiner, and Dow [14] first suggested that the disproportional
 95 expansion of the lateral cerebellum and the dentate cerebellar nuclei in human brain evolution
 96 (see text box 1) is due to its contributions to cognition. Since then, it has been shown that many
 97 cerebellar regions receive input from [15] and deliver output to [16,17] non-motor areas in
 98 parietal, prefrontal, temporal, and parahippocampal cortex. Indeed, it has been argued that the
 99 different cerebellar regions form closed and largely separated loops with many neocortical areas
 100 that are not directly implicated in motor control [18]. Consistent with these anatomical
 101 observations, patients with cerebellar damage sometimes do not demonstrate significant motor
 102 deficits, but instead (or additionally) exhibit a range of cognitive symptoms [19–21] that, while
 103 often more subtle than motor problems, are nonetheless replicable and robust. Moreover,
 104 functional neuroimaging studies have shown that the cerebellum reliably activates during most
 105 cognitive tasks [22–25]. Systematic mapping studies have revealed a detailed map of the
 106 functional specialization of the human cerebellum (Fig. 2a), with different subregions engaged in
 107 functions such as action observation, verbal and spatial working memory, executive functioning,
 108 language, social cognition, and even imagination [26].

109 But how does the cerebellum contribute to all these disparate cognitive functions? One
 110 enduring mystery is whether the cerebellum performs algorithmically similar computations

111 across motor and cognitive domains (a so-called “universal cerebellar transform”), or whether it
112 plays distinct computational roles across different domains. Moreover, linking these algorithmic
113 level questions to the circuit architecture of the cerebellum remains a difficult but critical task.

114 **A Universal Cerebellar Transform?**

115 The local micro-circuit of the cerebellar cortex is, relative to the neocortex, quite homogenous
116 across functional regions. This has led to the tempting idea that the cerebellum performs a
117 uniform computational function within each cortical-cerebellar loop. In essence, it has been
118 suggested that cognitive areas in the cerebellum modulate the activity of cortical association
119 areas to allow for ‘coordinated’ cognitive processes, in the same way that the motor areas of the
120 cerebellum modulate activity in primary motor cortex to allow for coordinated movements [27].

121 Despite the intuitive appeal of this idea, very little progress has been made to identify
122 what this universal function may be. The main hurdle has been to develop theories that are
123 formalized concretely enough to generate testable empirical predictions. In other brain regions,
124 such as the hippocampus, formal functional theories are starting to be developed. For example,
125 the computational framework of grid cell coding has been successfully applied not only to
126 navigation tasks in physical spaces, but also to cognitive tasks in conceptual spaces [28,29].

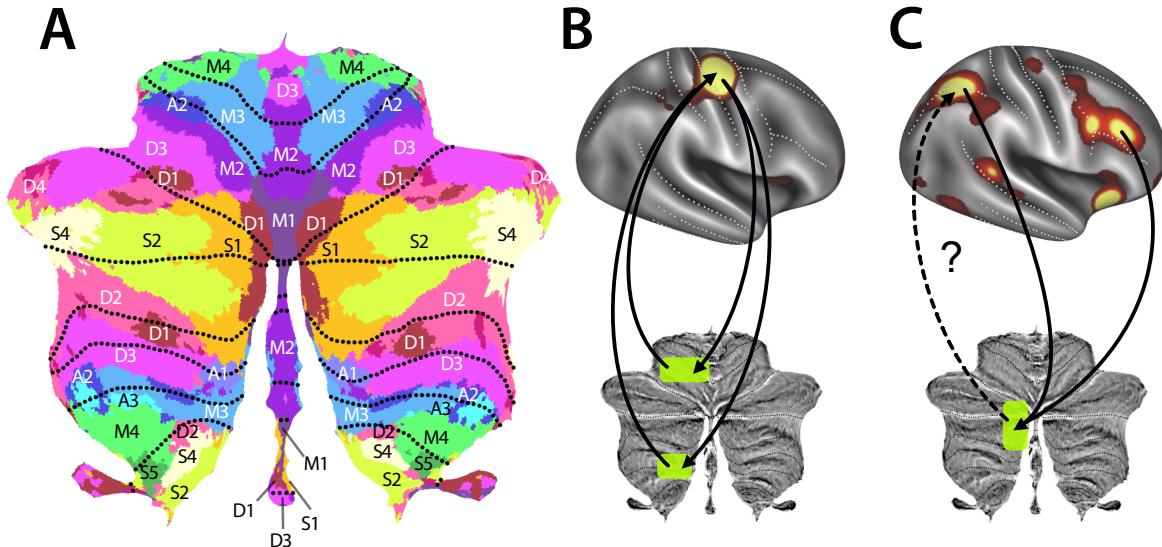
127 Why has it been so difficult to achieve something similar for the cerebellar circuit? One
128 possible answer is that the question “what is the function of the cerebellum?” does have not
129 have a more concrete answer than the question “what is the function of the neocortex?”. Indeed,
130 there is increasing evidence for differentiation in the microcircuitry across the cerebellum [30].
131 Furthermore, different cerebellar regions interact with cortical areas using potentially different
132 patterns of connectivity, such that the way the cerebellum influences cortical function may be
133 quite different across different cortical-cerebellar loops [31,32].

134 If this is true, then a more productive approach may be to investigate the contribution of
135 the cerebellum in each of the cortico-cerebellar loops separately first, without *a priori* assuming
136 that it serves the same function as in the neighboring loop. If there truly is a shared
137 computational principle that characterizes the cerebellar contribution across all these loops, it
138 will emerge with the data. In the remainder of the paper, we attempt to outline what specific
139 questions need to be resolved for each cortico-cerebellar loop to make concrete progress in
140 characterizing cerebellar function.

141 **How is the cerebellum connected to other brain regions?**

142 If the basic element of our investigation is the cortico-cerebellar loop, then we first need to
143 identify them. In the rodent and monkey brain, viral tracing techniques [17] are able to precisely
144 map multi-synaptic connections. Since these techniques are not available in the human brain,
145 most of what we know about cortico-cerebellar connectivity has been indirectly inferred from the
146 correlations of functional magnetic resonance imaging (fMRI) signals between the neocortex
147 and the cerebellum. Most studies of this type are based on resting-state data, starting with the
148 seminal work by Buckner et al. [33]. After subdividing the neocortex into distinct resting-state
149 networks, the authors generated a functional map of the cerebellum by assigning each
150 cerebellar voxel to the cortical network it was most correlated with. Later work replicated the
151 main features of this basic connectivity pattern using both resting-state [34,35] and task-based
152 activity maps [26,36]. Given that the cerebellar BOLD signal is likely to mostly reflect mossy

153 fiber inputs (and local processing of those inputs in the granule cell layer), but not the activity of
 154 the output of the cerebellar cortex [37], we hypothesize that the fMRI correlations are
 155 predominantly shaped by projections from neocortex to cerebellum, rather than revealing much
 156 about the projections from the cerebellum back to the neocortex.



157
 158 **Figure 2.** (A) Functional parcellation displayed on a flattened representation of the human cerebellar
 159 cortex [26]. The color assigned to each parcel is a representation of the activation profile across many
 160 different cognitive and motor tasks. Green and bluish areas activate for movements of different body parts
 161 (M1-M4) and for action observation (A1-A3). Red areas (D1-D4) for working memory and executive
 162 function and yellow areas (S1-S5) for social and language functions. (B) Closed-loop connectivity
 163 between the hand area of primary motor cortex (M1) and the superior and inferior hand motor region (M3)
 164 in the contralateral cerebellum. (C) Convergence of frontal and parietal cortical areas onto a spatial
 165 working memory region (D1) in the contralateral cerebellum. From fMRI analysis it remains unclear which
 166 cortical areas this region projects back to (dashed line).

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 168 Across different connectivity models, several clear insights have emerged. First, most of
 169 the cerebellar input arises from the contralateral cerebral hemisphere, consistent with the
 170 crossing of mossy fibers originating from the pontine nuclei, with a more modest degree of
 171 uncrossed input. Second, while nearly all cortical areas appear to be functionally connected to
 172 the cerebellum, there are considerable differences in the proportions of the cerebellum vs. the
 173 neocortex that are occupied by each cortico-cerebellar loop. For example, the cerebellar
 174 contributions to visual networks appear to be disproportionately small, whereas the size of the
 175 regions dedicated to executive functions (i.e., the fronto-parietal network) is disproportionately
 176 large [26,33,34]. Surprisingly, the size of motor-related regions in the cerebellum roughly
 177 matches their relative size in the neocortex. Third, a single cortical area often connects to
 178 multiple spatially non-contiguous regions of the cerebellum: For example, primary motor cortex
 179 is connected both with the superior (lobules V, VI) and inferior (lobules VIII) hand representation
 180 in the cerebellum (M3, Fig. 2b), and the default-mode network appears to be connected to 3
 181 distinct sub-regions in the cerebellum (S3 in crus I, crus II, lobule IX) [26,38,39]. Finally, it has
 182 been suggested that there is substantial convergence of multiple cortical areas onto the same

183 cerebellar region, and that this convergence is especially pronounced in the so-called 'cognitive
184 areas' of crus I and crus II (Fig. 2c, [36]). There is also evidence from tracing studies in the
185 mouse that suggest that each cerebellar area projects back to multiple cortical areas [40]. It is
186 therefore possible that the synchronized cerebellar input to these neocortical regions changes
187 the coherence of neuronal activity between them [41]. In this way, the cerebellum may help to
188 coordinate the communication between distal pairs of cortical regions, rather than fine-tuning
189 neural dynamics within a single region.

190 In general, accurate connectivity models between the cerebellum and the rest of the
191 brain are an essential tool if we want to understand the role of the cerebellum across domains,
192 as these models tell us which brain regions provide input to - and receive output from - each
193 specific cerebellar area. This knowledge is essential, because it allows us to analyze the neural
194 activity in each cerebellar region in the context of the neural activity measured in other regions
195 within the same cortico-cerebellar loop. Time delays and changes in representation of
196 information can provide insights into the computations that occur at each stage of the loop. For
197 functional imaging in humans, we now have task-invariant connectivity models that make
198 quantitative and testable predictions about the amount and exact pattern of cerebellar activity,
199 based solely on the neocortical data for same tasks [26,36]. Deviations from such predictions
200 indicate the that cerebellar fMRI activity is not just a linear function of its inputs, but rather
201 suggest task-dependent gating or transformation of those inputs, providing potentially critical
202 insights into specific cerebellar functions [42].

203 ***How is information coded in the granule cell layer?***

204 One special characteristic of the cerebellar circuit is the massive information expansion in the
205 granule cell layer. Each single mossy fiber contacts tens to hundreds of granule cells, and each
206 granule cell integrates input from 4-5 mossy fibers, often coming from different sources. Even if
207 the mossy-fiber to granule cell connectivity was entirely random, the vast numbers of granule
208 cells and the diversity of synaptic characteristics [43] ensure a powerful non-linear expansion of
209 the original input, which is well-suited for learning complex functions [44,45] – that is, for
210 performing *pattern separation*. This feature was the central tenet of Marr's original formulation of
211 why the cerebellum may be a powerful learning machine, and has been further developed in
212 recent papers [46,47].

213 Given that it is difficult to record from isolated granule cells (which are very small and
214 tightly packed), direct tests of this idea have been missing until very recently. While an initial
215 study showed negative findings [48], we are only now seeing the first direct evidence that the
216 granule cell layer may indeed perform a computation akin to non-linear function expansion.
217 These recent results indicate that the granule cell layer code is indeed high-dimensional [49],
218 and that it is sparse while also combining information from multiple modalities in a non-linear
219 fashion [50]. Nonetheless, the exact characteristics of the granule cell population code are only
220 now beginning to be revealed.

221 What might the cerebellar information expansion achieve for cognitive functions? One
222 possibility is that information processing in the mossy-fiber layer is especially useful to learn
223 precise non-linear functions of time using a rich set of temporal basis functions [46,51]. This has
224 been extensively demonstrated in basic sensorimotor tasks, such as eyeblink conditioning. In
225 this paradigm, the conditioned stimulus (e.g., auditory tone) activates the mossy fiber, followed

226 by an unconditioned stimulus (an airpuff to the eye), which in turn activates climbing fibers. In
227 this context, the granule cell layer creates a distributed temporal code through the diverse
228 response dynamics of individual granule cells. This allows Purkinje cells to learn the exact
229 parallel-fiber pattern that precedes the climbing fiber input, thereby building up a temporally
230 precise prediction of when the air puff will occur [47].

231 Where in the cognitive domain do temporally precise predictions matter? While many
232 cognitive processes seem to occur at slower timescales, there are examples in language
233 comprehension and during social interactions, where the exact timing of stimuli matters. For
234 example, genuine smiles are returned with a median latency of 750ms [52], and it is possible
235 that the cerebellum is involved in the production and perception of such precisely timed
236 behaviors. To test this idea, characterizing the importance of the temporal dimension across
237 cognitive and social tasks and probing the cerebellar involvement in them will be the next critical
238 step. It should also be noted, however, that some behaviors that rely on the cerebellar circuit do
239 not seem to require accurate timing [53–55], suggesting that the non-linear function expansion
240 may also be used for non-temporal information.

241 ***What information is carried by climbing fibers in cognitive tasks?***

242 Climbing fibers provide the main teaching signals that shape the output of the cerebellar cortex,
243 the firing rate of Purkinje cells. Across different sensorimotor tasks, it has been important to
244 understand what information climbing fibers convey, as it provides insights about what the
245 cerebellar circuit tries to learn or to predict. In most motor tasks, climbing fibers appear to
246 convey information about motor errors, which then the cerebellar learning mechanism can help
247 to compensate for. What do we know about climbing fiber signals in cognitive tasks?

248 Recent work in reward learning tasks has greatly expanded traditional conceptions of
249 climbing fiber signals. In one influential study, Heffley et al. [56] designed a task that required
250 rodents to learn, via reward feedback, novel sensorimotor associations between abstract visual
251 stimuli and actions. Climbing fibers appeared to convey task-specific predictions about reward
252 outcomes rather than signaling motor errors. The types of climbing fiber signals were diverse,
253 reflecting events like reward prediction errors, unexpected rewards, and reward omissions.
254 These and similar findings – both in rodents and non-human primates – suggest that cerebellar
255 climbing fibers flexibly encodes abstract, task-specific variables and contingencies, not only
256 motor errors.

257 Furthermore, climbing fiber signals often convey unsigned reward prediction errors (i.e.,
258 surprise) rather than signed signals. They also do not always distinguish between the sensory
259 cues that differentially predict reward, even when the animal differentiates those cues
260 behaviorally [57]. Therefore, these signals do not fit well with the notion that climbing fibers carry
261 a specific and signed prediction error that can be used as a teaching signal for supervised
262 learning. Thus, further work is needed to better understand the role of climbing fiber signals, by
263 studying a wider range of cognitive tasks in rodents and non-human primates.

264 However, some cerebellar functional domains - such as language [58] - will be difficult or
265 impossible to study in animal models. In these cases, it is even less clear what information is
266 carried by climbing fibers. Therefore, it is also essential to develop improved techniques of
267 measuring inferior olive activity using non-invasive methods in humans. Despite a few
268 encouraging reports [59–61], fMRI of the inferior olive remains extremely difficult given the

269 reduced signal-to-noise ratio, spatial distortions, and artifacts induced by the cardiac cycle [62].
270 Solving these problems and demonstrating reliable, spatially specific activity within the inferior
271 olive across different domains would be a great step forward in understanding the role of the
272 cerebellum in cognitive tasks: The nature of the climbing fiber input will inform us about what the
273 cerebellar circuitry is trying to learn.

274 ***How does cerebellum modulate neural dynamics in the neocortex?***

275 Cerebellar output contributes to cognitive functions by modulating the dynamics of recurrent
276 activity in the neocortex via modulation of the thalamus. If there is a common principle of
277 cerebellar function across domains, it must be found in how it affects thalamo-cortical activity
278 dynamics. To glean insights into this process, several labs have started to apply temporally
279 precise perturbations of cerebellar activity while measuring the resulting influence on behavior
280 and cortical activity. For example, a study in mice [63] showed that cerebellar output to the
281 anterior lateral motor area (a neocortical premotor structure) is essential for sustaining the
282 preparatory neural signals associated with motor planning. Delay-period motor planning could
283 be causally disrupted by perturbing cerebellar output, without interfering with the execution of
284 movements. Similar results were also found in a task that required the accumulation of sensory
285 evidence to guide perceptual decision making [64]. These results indicate that cerebellar output
286 may be important for the maintenance and dynamic updating of neocortical representations of
287 abstract internal goals or decision variables.

288 Superficially, a role in maintaining cortical representations that evolve at a relatively slow
289 time scale does not fit well with the idea that the cerebellum is critical for regulating the precise
290 temporal dynamics necessary for many motor behaviors [46,47]. Observing the influence of
291 cerebellar disruption on thalamo-cortical activity across a wider range of tasks will be critical for
292 identifying whether there is a common dynamic motive across cerebellar-cortical loops, or if the
293 temporal constraints on cerebellar contributions are in fact looser than commonly believed.

294 ***What is the cerebellum's role in cognitive development?***

295 Perinatal lesions to the cerebellum have profound impact on motor, language, and cognitive
296 development [65,66] and dramatically increase the likelihood of an autism diagnosis [67]. The
297 resection of parts of the cerebellum during childhood can cause a complete or partial cessation
298 of speech, a symptom called cerebellar mutism [68]. Importantly, equivalent lesions in adulthood
299 do not cause similar symptoms, or if they do, lead to much milder deficits. These facts contrast
300 directly with what is observed for lesions of the neocortex; for example, early lesions to
301 language-related regions can lead to substantial reorganization and recovery of function,
302 whereas the same lesion in adulthood leads to lasting deficits.

303 These observations have led to the idea that the cerebellum helps to 'set up' neocortical
304 circuits underlying cognition in development [67]. If the cerebellum is lesioned during this critical
305 period, development is delayed – however, once the neocortical regions have been established,
306 the same cerebellar circuit may not be necessary anymore. This idea has also been extended to
307 the ageing brain. Here the cerebellum may play a neuroprotective role – for example, it may
308 help to reorganize cortical circuits to compensate for tissue loss in the earlier stages of
309 dementia [69].

310 While compelling, this idea is unlikely to provide a complete characterization of
311 cerebellar function in general. Lesions to cerebellar motor areas lead to profound ataxia both in
312 children [68] and adults – indicating that the cerebellum sometimes provides functions that
313 cannot easily be replaced by a well-trained neocortex.

314 **Concluding remarks**

315 Despite a wealth of knowledge about the cerebellar circuit itself, a general theory of how the
316 cerebellum contributes to both cognition and motor control has remained elusive. In this paper
317 we argue that cerebellar output may contribute to function in different ways depending on the
318 system it is embedded in. This makes it necessary to study different cortico-cerebellar loops,
319 especially those involved in cognitive function, without the *a priori* assumption that the results
320 will generalize across loops directly.

321 Taking a systems-level view also implies that it will be difficult to understand the
322 contributions of the cerebellum to cognition before we have better models of how cognitive
323 functions arise from the neuronal dynamics across different cortical regions. A possible recipe
324 for scientific progress involves three necessary steps: First, for a cerebellar region of interest,
325 we need to characterize the sources of inputs and the targets of outputs, both in the thalamus
326 and neocortex. Secondly, it will be important to record activity in as many brain areas in this
327 loop as possible and see how they relate to one another and to the task of interests, and how
328 information is manipulated across the loop. Finally, targeted perturbations in selected structures
329 with simultaneous recordings in others will provide the critical data to disambiguate between
330 different network models. While this all sounds extremely ambitious, technological advances in
331 recording and stimulation are finally bringing such studies into reach [70].

332 Given these new data, what will a theory of cerebellar function in cognition finally look
333 like? One key element will be to build biologically constrained computational models of
334 cerebellar circuit function (for a recent example, see [42]). These models may be built by fitting
335 neural data from sensorimotor task, but the cerebellar circuit could then be recombined with a
336 model of cortical association areas. It will be enlightening to see to what degree the function of
337 the same circuitry changes when embedded in a system with different task representations and
338 neural dynamics. Ultimately, such models should be able make specific predictions about the
339 influence (or non-influence) of cerebellar disruptions onto cognitive tasks that can then be tested
340 directly. Theory driven studies like this would be one sign of significant progress.

341 **Text Box: What do seals, elephants, bats, crows, and humans have in common?**
342 The genetic blueprint for a fully developed cerebellum appeared first in jawed fish and is
343 common to all vertebrates descending from this common ancestor [72]. From then on, there
344 was a tendency of the cerebellum to enlarge in proportion with the rest of the brain. However,
345 for some species the overall cerebellum has enlarged to an unusual degree, for example for
346 weakly electric fishes (Mormyridae [73]), elephants [74], bats [75], crows and other large-
347 brained birds [75]. Other species show a specific enlargement of the cerebellar hemispheres
348 over the vermis, as for example in seals (pinnipeds), dolphins (cetaceans [76]), and apes
349 (including humans [77]). Importantly, these adaptations cannot be traced to a common ancestor
350 but appear on unconnected branches of the evolutionary tree. This suggests that at multiple
351 times in evolutionary history there existed selective pressures for which a large cerebellum
352 provided a competitive solution and increased fitness. What problem the cerebellar circuit was
353 able to solve in each case, however, appears to vary widely across the animal kingdom, and
354 includes functions such as electric sensing, echo location, vocal learning, complex social
355 behavior, control of a flexible trunk, skilled object manipulation (with beak or hand), and,
356 especially in humans, higher cognitive functions. Why did these functions (and not others)
357 depend on a large cerebellum? For example, what is special about the control of a flexible trunk
358 that has led to cerebellar enlargement in elephants and weakly electric (or elephant) fish in
359 parallel? How did a creature like an octopus solve a similar biomechanical problem of controlling
360 its arms without a cerebellum? Studies of distantly related animals that show similar behavioral
361 adaptations associated with the use of increased cerebellar territory may provide insight into the
362 computational characteristics of problems that the cerebellar circuit is especially good at solving.
363 From evolutionary history we know that the answer to this question cannot be a simple one and
364 must account for an astounding variety of behaviors.

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